

21EC54

Fifth Semester B.E./B.Tech. Degree Examination, June/July 2025

Electromagnetic Waves

Time: 3 hrs. Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

## Module-1

- a. What do you mean by scalar and vector fields? Show the difference between two. (06 Marks)
  - b. Given three points in Cartesian coordinate system as A(3, -2, 1), B(-3, -3, 5), C(2, 6, -4). Find: i) The vector from A to C
    - ii) The unit vector from B to A
    - iii) The distance from B to C
    - iv) The vector from A to the midpoint of the straight line joining B to C. (08 Marks)
  - c. State Coulomb's law of force between any two point charges and also in vector form.

(06 Marks)

#### OR

- 2 a. A charge  $Q_2 = 12$  inc is located in free space at  $P_2$  (-0.03, 0.01, 0.04)m. Find the force on  $Q_2$  due to  $Q_1$  where  $Q_1 = 110\mu C$  at  $P_1(0.03, 0.08, -0.02)m$ . (06 Marks)
  - b. A volume charge density is expressed as  $\rho_v = 10z^2 x \sin \pi y$ . Find the total charge inside the volume  $(-1 \le x \le 2)$ ,  $(0 \le y \le 1)$ ,  $(3 \le z \le 3.6)$ .
  - c. Derive the expression for electric field intensity due to infinite line charge. (08 Marks)

#### Module-2

a. State and prove the Gauss's law.

- (06 Marks)
- b. Consider a coaxial cable with inner radius 'a' and outer radius 'b'. Derive the expression for flux density  $(\overline{D})$  for the region a < r < b using Gauss's law. (08 Marks)
- c. The flux density  $\overline{D} = r/3 \ \overline{a}_r \ nc/m^2$  is in the free space:
  - i) Fine  $\overline{E}$  at r = 0.2m
  - ii) Find the electric flux leaving the sphere of r = 0.2m.
  - iii) Find the total charge within the sphere of r = 03.m.

(06 Marks)

#### OR

- 4 a. Derive Maxwell first equation as applied to the electro statics, using Gauss's law. State the divergence theorem using Maxwell's first equation. (06 Marks)
  - b. Evaluate the both sides of divergence theorem for the field  $\overline{D} = 2xy \ \overline{a}_x + x^2 \ \overline{a}_y \ c/m^2$  and rectangular parallel piped formed by the planes x = 0 and x = 1, y = 0 and y = 2 and z = 0 and z = 3.
  - c. Derive the expression for the work done in moving a point charge in an electric field.

    (06 Marks)

## Module-3

- 5 a. Determine whether or not the following potential fields satisfy the Laplace's equation: i)  $V = x^2 - y^2 + z^2$  ii)  $V = r \cos \phi + z$  iii)  $V = r \cos \phi + \phi$ . (06 Marks)
  - b. Using the Laplace's equation, derive an expression for capacitance per unit length of a coaxial cable using the following boundary conditions.  $V = V_0$  at r = a and V = 0 at r = b, b > a. (08 Marks)
  - c. State and explain Biot Savart law applicable to magnetic field. (06 Marks)

## OR

- 6 a. Derive the expression for a curl, applying Ampere's circuital law to an incremental surface element. (08 Marks)
  - b. State and prove the Stoke's theorem. (06 Marks)
  - c. What is scalar magnetic potential? Explain Laplace equations for scalar magnetic potential.
    (06 Marks)

## Module-4

- 7 a. Define and explain the terms magnetic flux and magnetic flux density. Obtain the magnetic flux using magnetic flux density in coaxial cable. (08 Marks)
  - b. In certain region, the magnetic flux density in a magnetic material with  $\chi_m=6$  is given and  $\overline{B}=0.005y^2$   $\overline{a}_x$  T. At y=0.4m, find the magnitude of: i)  $\overline{J}$  ii)  $\overline{J}_b$  iii)  $\overline{J}_T$ . (06 Marks)
  - c. Discuss the boundary conditions for magnetic field based on the normal component of the  $\overline{B}$  and  $\overline{H}$ . (06 Marks)

# OR

- 8 a. Derive an expression for the magnetic force between differential current elements. (06 Marks)
  - b. A conductor of length 2.5m in z=0 and x=0 carries a current of 12A in  $-\overline{a}_y$  direction. Calculate the uniform flux in the region, if the force on the conductor is  $12 \times 10^{-2}$  N in the direction specified by  $\left[\frac{-\overline{a}_x + \overline{a}_z}{\sqrt{2}}\right]$ . (08 Marks)
  - c. State and explain Faraday's law of electromagnetic induction in integral and point form.
    (06 Marks)

# Module-5

- 9 a. Write the Maxwell's equations in the integral form and explain the physical significance.
  - b. Two parallel conducting plates of area  $0.05\text{m}^2$  are separated by 2mm of lossy, dielectric for which  $\epsilon_r = 8.3$  and  $\sigma = 8 \times 10^{-4}$  S/m. given an applied voltage  $V = 10 \sin 10^7$  t V. Find total r.m.s current.
  - c. Do the fields  $E = E_m \sin x \sin t \ \overline{a}_y$  and  $\overline{H} = \frac{E_m}{\mu o} \cos x \cos t \ \overline{a}_z$  satisfy the Maxwell's equations. (06 Marks)

#### OR

- 10 a. Write short notes on Retarded potential. (06 Marks)
  - b. Given  $E = E_0 z^2 e^{-t} \overline{a}_x$  in free space, determine if there exist a magnetic field such that both Faraday's law and Ampere's circuital law are satisfied simultaneously. (08 Marks)
  - c. Discuss the propagation of uniform plane wave in good conductor. (06 Marks)