

Fifth Semester B.E. Degree Examination, June/July 2025 Automata Theory and Computability

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Define the following terms with example : i) Alphabet ii) Power of an alphabet
iii) String iv) Language v) Kleene star. (05 Marks)
- b. Design DFSM for each of the following languages :
i) $L = \{W : W \text{ has even number of a's and even number of b's}\}$.
ii) $L = \{W : |W| \bmod 5 \neq 0\}$ on $\Sigma = \{a, b\}$. (10 Marks)
- c. Mention the differences between DFSM, NFSM and ϵ -NFSM. (05 Marks)

OR

- 2 a. Define Distinguishable and Indistinguishable states. Minimize the following DFSM.

δ	$\rightarrow A$	B	*C	D	E	F	G	H
0	B	G	A	C	H	C	G	G
1	F	C	C	G	F	G	E	C

- b. Convert the following NDFSM to DFSM. Refer Fig. Q2(b).

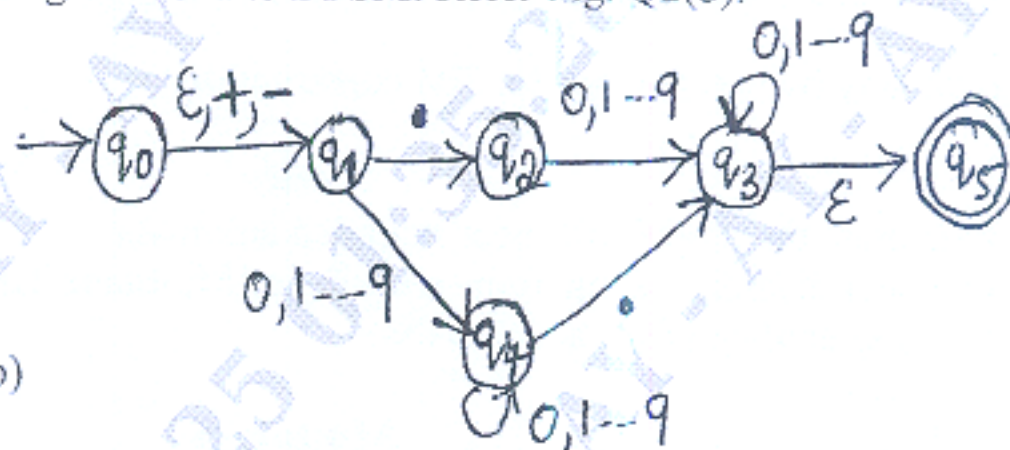


Fig. Q2(b)

Module-2

- 3 a. Define Regular Expression. Write Regular Expression for the following languages :
i) $L = \{a^{2n} b^{2m} \mid n \geq 0, m \geq 0\}$ ii) $L = \{a^n b^m \mid n \geq 4, m \leq 3\}$
iii) $L = \{W \in \{a, b\}^* : \text{strings with alternate a's and b's}\}$. (08 Marks)
- b. Obtain ϵ -NDFSM for the regular expression $a^* + b^* + c^*$. (06 Marks)
- c. Build a Regular expression from an FSM. Refer Fig. Q3(c). (06 Marks)



Fig. Q3(c)

OR

- 4 a. State and prove Pumping lemma theorem for regular languages. Show that $L = \{WW^R \mid W \in (0+1)^*\}$ is not regular. (10 Marks)
- b. Show that if L_1 and L_2 are regular, then $L_1 \cup L_2$, $L_1 \cdot L_2$ and L_1^* are also regular. (06 Marks)
- c. Write Regular Grammar & FSM for the language $L = \{W \in \{a, b\}^* : W \text{ ends with Pattern } aaaa\}$. (04 Marks)

Module-3

- 5 a. Define CFG and design a CFG for the following Languages :
 i) $L = \{a^n b^{n+2} : n \geq 0\}$
 ii) $L = \{WW^R \mid W \in (a, b)^*\}$
 iii) $L = \{0^i 1^j \mid i \neq j, i \geq 0 \text{ and } j \geq 0\}$. (10 Marks)
- b. Define CNF. Convert the following CFG into CNF.
 $S \rightarrow aACa \quad A \rightarrow B \mid a \quad B \rightarrow C \mid c \quad C \rightarrow cC \mid \epsilon$ (10 Marks)

OR

- 6 a. Design a PDA for the language $L = \{a^n b^n \mid n \geq 0\}$ and show the moves made by PDA for the string aaabbb. (10 Marks)
- b. Define Leftmost derivation, Rightmost derivation and Parse tree. Consider the grammar.
 $E \rightarrow E + E \mid E * E \mid E - E \mid E \rightarrow id$. Obtain LMD, RMD and Parse tree for the string $id + id * id$. (10 Marks)

Module-4

- 7 a. Design a TM for the language $L = \{1^n 2^n 3^n \mid n \geq 1\}$. Show that 112233 is accepted by ID. (12 Marks)
- b. Explain any two techniques for TM construction. (08 Marks)

OR

- 8 a. Demonstrate the model of Linear bounded automata. (08 Marks)
- b. With a neat diagram, explain the working of Multitape Turing M/C. (08 Marks)
- c. Define and explain DTM and NDTM. (04 Marks)

Module-5

- 9 a. Explain the following with example :
 i) Decidability ii) Decidable Languages iii) Undecidable languages. (12 Marks)
- b. Explain Halting problem in TM. (08 Marks)

OR

- 10 a. Explain Quantum computers. (07 Marks)
- b. Explain P and NP classes. (07 Marks)
- c. Write applications of TM (06 Marks)

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