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BMATC201

Second Semester B.E./B.Tech. Degree Examination, Dec.2024/Jan.2025
Mathematics – II for Civil Engineering Stream

Time: 3 hrs.

Max. Marks: 100

- Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.*
2. VTU Formula Hand Book is permitted.
3. M : Marks , L: Bloom's level , C: Course outcomes.

Module – 1				M	L	C
Q.1	a.	Evaluate $\int_0^1 \int_x^{\sqrt{x}} (x^2 + y^2) dy dx$.		7	L2	CO1
	b.	Evaluate $\int_0^a \int_y^a \frac{x}{x^2 + y^2} dx dy$ by changing the order of integration.		7	L3	CO1
	c.	Derive the relation $\beta(m, n) = \frac{\gamma(m) \cdot \gamma(n)}{\gamma(m+n)}$.		6	L2	CO1
OR						
Q.2	a.	Evaluate $\int_{-a}^a \int_0^{\sqrt{a^2 - x^2}} \sqrt{x^2 + y^2} dy dx$ by changing into polar coordinates.		7	L3	CO1
	b.	Using double integration find the area of a plane in the form of a quadrant of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$.		7	L2	CO1
	c.	Using modern mathematical program to evaluate the integral, $\int_0^3 \int_0^{3-x} \int_0^{3-x-y} xyz dz dy dx$.		6	L3	CO5
Module – 2						
Q.3	a.	If $\vec{F} = \nabla(xy^3z^2)$, find $\text{div } \vec{F}$ and $\text{curl } \vec{F}$ at the point (1, -1, 1).		7	L2	CO2
	b.	Define an irrotational vector. Find the constants a, b, c such that $\vec{F} = (x + y + az)\mathbf{i} + (bx + 2y - z)\mathbf{j} + (x + cy + 2z)\mathbf{k}$ is irrotational.		7	L2	CO2
	c.	Find the directional derivative of $\phi = x^2yz + 4xz^2$ at the point (1, -2, -1) in the direction of the vector $2\hat{i} - \hat{j} - 2\hat{k}$.		6	L2	CO2

OR																	
Q.4	a.	Using Green's theorem, evaluate $\oint (3x^2 - 8y^2)dx + (4y - 6xy)dy$, where C is the boundary of the region enclosed by $y = \sqrt{x}$ and $y = x^2$.	7	L3	CO2												
	b.	If $\vec{F} = xy\hat{i} + yz\hat{j} + zx\hat{k}$, evaluate $\int_C \vec{F} \cdot d\vec{r}$ where C is the curve represented by, $x = t, y = t^2, z = t^3 - 1 \leq t \leq 1$	7	L2	CO2												
	c.	Write the modern mathematical tool program to find the divergence of the vector field, $\vec{F} = x^2yz\hat{i} + y^2xz\hat{j} + z^2xy\hat{k}$.	6	L3	CO5												
Module – 3																	
Q.5	a.	Form the partial differential equation by eliminating the arbitrary function from the relation, $\ell x + my + nz = f(x^2 + y^2 + z^2)$	7	L2	CO3												
	b.	Solve $\frac{\partial^2 z}{\partial y^2} = Z$, given that $y = 0, z = e^x$ and $\frac{\partial z}{\partial y} = e^{-x}$.	7	L3	CO3												
	c.	Solve $x(y^2 - z^2)p + y(z^2 - x^2)q = z(x^2 - y^2)$ using Lagrange's multipliers.	6	L2	CO3												
OR																	
Q.6	a.	Form the partial differential equation by eliminating the arbitrary constants from $(x - a)^2 + (y - b)^2 + z^2 = C^2$.	7	L2	CO3												
	b.	Solve $\frac{\partial^2 z}{\partial x \partial y} = \sin x \sin y$ for which $\frac{\partial z}{\partial y} = -2 \sin y$, when $x = 0$ and $z = 0$ if y is an odd multiple of $\frac{\pi}{2}$.	7	L3	CO3												
	c.	Derive one dimensional wave equation.	6	L2	CO3												
Module – 4																	
Q.7	a.	By Newton's-Raphson method find the root of $x \sin x + \cos x = 0$, which is near to $x = \pi$.	7	L2	CO4												
	b.	The population of a town is given by the following table : <table border="1"> <tr> <td>Year</td><td>1951</td><td>1961</td><td>1971</td><td>1981</td><td>1991</td></tr> <tr> <td>Population</td><td>19.96</td><td>39.65</td><td>58.81</td><td>72.21</td><td>94.61</td></tr> </table> Using Forward and Backward Newton's interpolation formula, calculate the increase in population between the years 1955 to 1985.	Year	1951	1961	1971	1981	1991	Population	19.96	39.65	58.81	72.21	94.61	7	L2	CO4
Year	1951	1961	1971	1981	1991												
Population	19.96	39.65	58.81	72.21	94.61												
	c.	Evaluate $\int_0^{\frac{\pi}{2}} \sqrt{\cos \theta} d\theta$ by taking 7 ordinates using Simpson's $\left(\frac{1}{3}\right)^{rd}$ rule.	6	L3	CO4												

OR

OR															
Q.8	a.	Compute the real root of the equation $x \log_{10} x - 1.2 = 0$ by the Regula Falsi method taking Four decimal places.	7	L2	CO4										
	b.	Compute the value of y when $x = 4$, using Lagrange's interpolation formula given, <table border="1"><tr><td>x</td><td>0</td><td>2</td><td>3</td><td>6</td></tr><tr><td>f(x)</td><td>-4</td><td>2</td><td>14</td><td>158</td></tr></table>	x	0	2	3	6	f(x)	-4	2	14	158	7	L2	CO4
x	0	2	3	6											
f(x)	-4	2	14	158											
	c.	Evaluate $\int_0^{0.3} (1 - 8x^3)^{\frac{1}{2}} dx$ by using Simpson's $\left(\frac{1}{3}\right)^{\text{rd}}$ rule, by taking 3 equal parts.	6	L3	CO4										

Module – 5

Q.9	a.	Solve by using modified Euler's method. $\frac{dy}{dx} = x - y^2$, $y(0) = 1$ taking $h = 0.1$, find $y(0.2)$.	7	L2	CO4
	b.	Applying Milne's predictor and corrector method, find $y(0.8)$ from $\frac{dy}{dx} = x - y^2$ and given $y(0) = 0$, $y(0.2) = 0.02$, $y(0.4) = 0.0795$, $y(0.6) = 0.1762$.	7	L2	CO4
	c.	Using Runge-Kutta method of order 4, find y at $x = 0.1$, given that $\frac{dy}{dx} = 3e^x + 2y$, $y(0) = 0$ and $h = 0.1$.	6	L3	CO4

OR

Q.10	a.	Use Taylor's series method to find $y(0.1)$ from $\frac{dy}{dx} = x - y^2$ and $y = 1$ at $x = 0$ upto 4 th degree.	7	L2	CO4
	b.	Using the Runge-Kutta method of order 4, solve $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$ with $y(0) = 1$ at $h = 0.2$, find $y(0.2)$.	7	L2	CO4
	c.	Using mathematical tools, write a code to find the solution of $\frac{dy}{dx} = 1 + \frac{y}{x}$ at $y(2)$ taking $h = 0.2$ given that $y(1) = 2$ by Runge-Kutta method of order 4.	6	L3	CO5
