# Sixth Semester B.E./B.Tech. Degree Examination, Dec.2024/Jan.2025 Signals and Digital Signal Processing

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

# Module-1

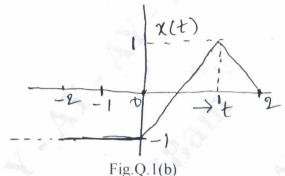
1 a. For the following discrete time systems, determine whether the system is: i) Linear ii) Time invariant iii) Memory less iv) Causal v) Stable.

I) y(n) = x(1-n)

II)  $y(n) = \log_{10}^{(|x(n)|)}$ 

(06 Marks)

b. Sketch the even and odd component of the continuous time signal x(t) shown in Fig.Q.1(b) (06 Marks)



Consider an LTI system with unit impulse response h(t) = u(-t + 2). If the input applied to the system is x(t) = u(t + 2) - u(t - 1) find the output y(t) of the system. (08 Marks)

#### OR

- 2 a. Consider an LTI system with input  $x(n) = 2^n u(-n)$  and impulse response h(n) = u(n). Compute the output of the system y(n) and also plot it. (10 Marks)
  - b. Check whether the following discrete time signals are energy or power signals:

i) 
$$x(n) = \begin{cases} 3(-1)^n; & n \ge 0 \\ 0; & n < 0 \end{cases}$$
 ii)  $x(n) = A\delta(n)$  (06 Marks)

c. Find the step response for the LTI system represented by  $h(t) = e^{-|t|}$ . (04 Marks)

# Module-2

- 3 a. Let x(n) be a finite length sequence with  $X(K) = \{10, -2 + j2, -2, -2 j2\}$ . Using the properties of DFT find the DFT<sup>s</sup> of the following sequences

  i)  $x_1(n) = x((n + 2))_4$ ii)  $x_2(n) = x(4 n)$ .
  - b. Prove the periodic property of DFT.

(02 Marks)

c. Using overlap save method, compute y(n) of a FIR filter with impulse response  $h(n) = \{3, 2, 1\}$  and input  $x(n) = \{2, 1, -1, -2, -3, 5, 6, -1, 2, 0, 2, 1\}$  (10 Marks)

#### OR

a. Using frequency domain approach, compute the energy of the 4 point sequence

$$x(n) = \sin\left(\frac{2\pi}{N}n\right), \ 0 \le n \le 3$$
 (08 Marks)

State and prove the following properties of DFT i) Time reversal ii) Circular convolution iii) Multiplication.

# Module-3

- Develop an 8-point decimation in frequency FFT algorithm. Draw the complete signal flow 5 graph. (10 Marks)
  - b. Find 4 point circular convolution of x(n) and h(n) using radix-2 DIF-FFT algorithm.  $x(n) = \{1, 1, 1, 1\}, h(n) = \{1, 0, 1, 0\}.$ (10 Marks)

## OR

- 6 2 - j2, 0}; Determine the remaining points. Hence find the sequence x(n) using DIF-FFT algorithm. (10 Marks)
  - b. Why FFT is needed? Explain the classification of FFT algorithms. (05 Marks)
  - c. List any two similarities and differences between DIT and DIF algorithms. (05 Marks)

## Module-4

- Design a chebyshev analog filter with ripple of 0.5dB in the passband  $|\Omega| \le 1$  and at  $\Omega = 3$ , amplitude is down by 3dB. (10 Marks)
  - b. Obtain H(z) using impulse invariance method for following analog filter.

$$H_a(s) = \frac{1}{(s+0.5)(s^2+0.5s+2)}$$
 (10 Marks)

## OR

- a. Explain the frequency transformation in analog filters. (06 Marks)
  - b. List the advantages and disadvantages of digital filter. (04 Marks)
  - Design a unit band width 3dB digital Butterworth filter of first order by using bilinear transformation. (10 Marks)

# Module-5

- a. Obtain the direct form I, direct form II, cascade and parallel form realization for the 9 following system y(n) = 0.75y(n-1) - 0.125y(n-2) + 6x(n) + 7x(n-1) + x(n-2).
  - (14 Marks) b. List the advantages and disadvantages of FIR filters. (06 Marks)

Design the symmetric FIR lowpass filter whose desired frequency response is given as  $H2(w) = \begin{cases} e^{-jwt} & \text{for } |w| \leq w_c \\ 0; & \text{other wise} \end{cases}$ **10** a.

$$H2(w) = \begin{cases} e^{-jwt} & \text{for } |w| \le w_c \\ 0; & \text{other wise} \end{cases}$$

The length of the filter should be 7 and  $w_c = 1$  rad/sample. Use rectangular window.

(10 Marks)

b. Realize the following system function in i) Direct form ii) Cascade form

$$H(z) = 1 + \frac{3}{4}z^{-1} + \frac{17}{8}z^{-2} + \frac{3}{4}z^{-3} + z^{-4}$$
 (10 Marks)