

Fifth Semester B.E./B.Tech. Degree Examination, Dec.2024/Jan.2025

Finite Element Analysis

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Explain the steps involved in finite element method to solve engineering problems. (10 Marks)
- b. With an example, explain node numbering scheme and node location system. (10 Marks)

OR

- 2 a. Explain simplex, complex and multiplex elements with examples. (10 Marks)
- b. Determine the displacement at the nodes for spring mass system shown in Fig Q2(b), using principle of minimum potential energy. Take $F_1 = 60 \text{ N}$, $F_2 = 50 \text{ N}$. (10 Marks)

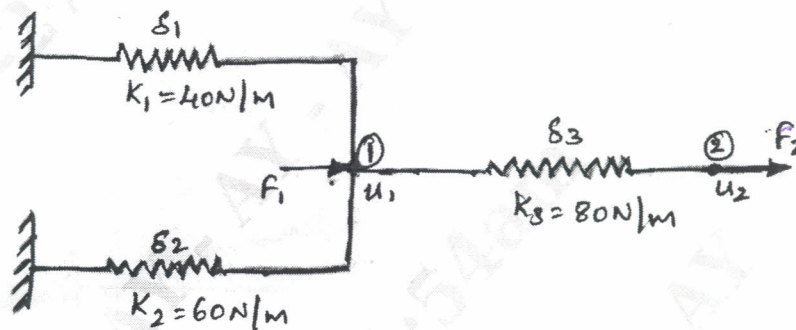


Fig Q2(b)

Module-2

- 3 a. Derive the elemental stiffness matrix for 1D bar element. (10 Marks)
- b. For the two bar truss shown in Fig Q3(b), determine the nodal displacement and stress in element 1, Take, $E = 2 \times 10^5 \text{ N/mm}^2$, $A = 200 \text{ mm}^2$.

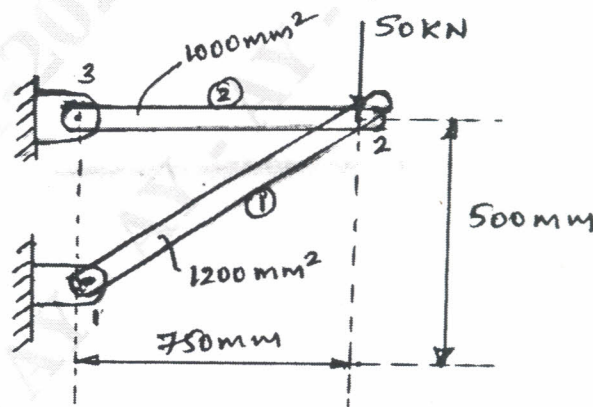
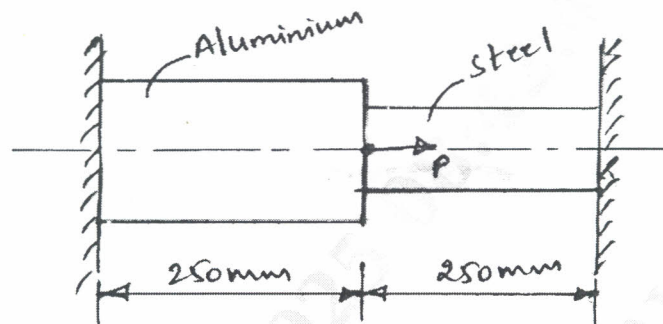


Fig Q3(b)

(10 Marks)

OR

- 4 Determine the stresses in members of structure given below in Fig Q4, using penalty approach of handling boundary conditions.



Given/Take

$$P = 4000 \text{ N}$$

$$A_1 = 1600 \text{ mm}^2$$

$$A_2 = 800 \text{ mm}^2$$

$$E_{Al} = 80 \text{ GPa}$$

$$E_{steel} = 210 \text{ GPa}$$

Fig Q4

(20 Marks)

Module-3

- 5 a. Derive Hermite shape function for beam element. (10 Marks)
 b. Fig Q5(b), shows a simply supported beam subjected to a uniformly distributed load. Obtain the maximum deflection. Take $E = 200 \text{ GPa}$, $I = 2 \times 10^6 \text{ mm}^4$.

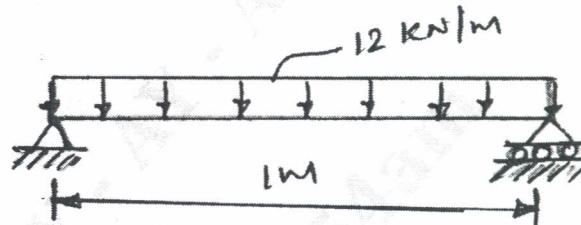


Fig Q5(b)

(10 Marks)

OR

- 6 a. Derive stiffness matrix for torsion of shaft. (10 Marks)
 b. A bar of circular cross section having a diameter of 50 mm is firmly fixed at its ends and subjected to a torque at B and C as shown in Fig Q6(b). Determine maximum angle of twist and shear stress. Take $G = 7 \times 10^4 \text{ N/mm}^2$ and $E = 2 \times 10^5 \text{ N/mm}^2$.

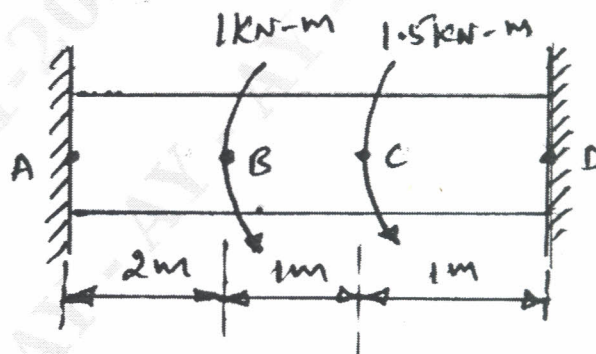


Fig Q6(b)

(10 Marks)

Module-4

- 7 Determine the temperature distribution in the composite wall using 1D heat element, use penalty approach of handling boundary condition.
 Take : $K_1 = 25 \text{ W/m}^\circ\text{C}$, $K_2 = 35 \text{ W/m}^\circ\text{C}$, $K_3 = 55 \text{ W/m}^\circ\text{C}$, $h = 30 \text{ W/m}^2 \text{ }^\circ\text{C}$, $T_\infty = 900^\circ\text{C}$, $A = 1 \text{ m}^2$.

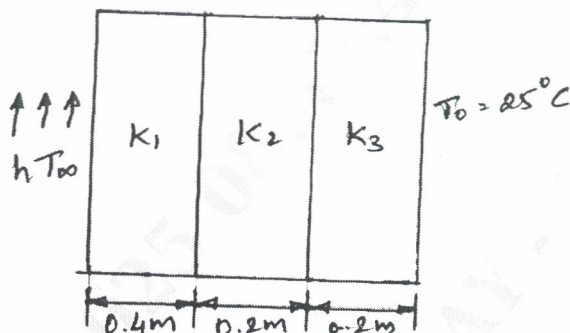


Fig Q7

(20 Marks)

OR

- 8 For the smooth pipe shown in Fig Q8, with uniform c/s of 1 m^2 , determine the flow velocities at the centre and right end, knowing the velocity at the left is $V_x = 2 \text{ m/s}$.

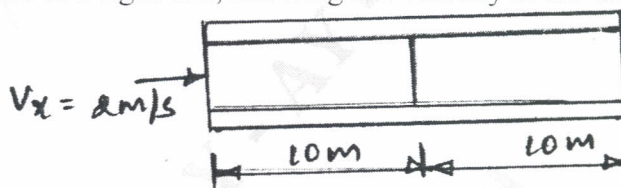


Fig Q8

(20 Marks)

Module-5

- 9 a. Derive stiffness matrix of axi-symmetric bodies with triangular elements. (10 Marks)
 b. For the element of an axisymmetric body rotating with a constant angular velocity $W = 1000 \text{ rev/min}$ as shown in Fig Q9(b). Determine the body force vector. Include the weight of the material, where the specific density is 7850 Kg/m^3 .

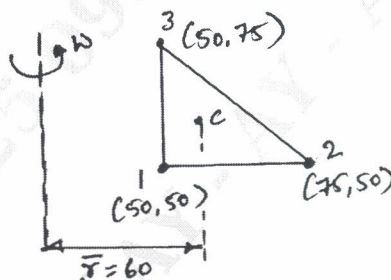


Fig Q9(b)

(10 Marks)

OR

- 10 a. Derive an equation for lumped mass matrix for 1D bar element. (10 Marks)
 b. Determine the natural frequency of vibration of the cantilever beam shown in Fig Q10(b). Take $E = 200 \text{ GPa}$, $\rho = 7840 \text{ Kg/m}^3$, $I = 2000 \text{ mm}^4$, $A = 240 \text{ mm}^2$. (10 Marks)

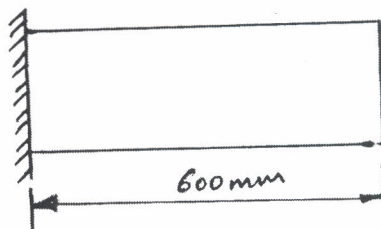


Fig Q10(b)

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