

17MAT21

Second Semester B.E. Degree Examination, June/July 2024 **Engineering Mathematics - II**

Time: 3 hrs. Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

1 a. Solve
$$(D^2 + 1)y = 3x^2 + 6x + 12$$
. (06 Marks)

b. Solve
$$(D^3 + 2D^2 + D)y = e^{-x}$$
. (07 Marks)

c. By the method of undetermined coefficients, solve
$$(D^2 + D - 2)y = x + \sin x$$
. (07 Marks)

2 a. Solve
$$(D^2 - 6D + 9)y = 6e^{3x} + 7e^{-2x}$$
. (06 Marks)

b. Solve
$$(D^3 - D)y = (2x + 1) + 4\cos x$$
. (07 Marks)

c. By the method of variation of parameters, solve
$$(D^2 + 1)y = \csc x$$
. (07 Marks)

Module-2

3 a. Solve
$$(x^2D^2 + xD + 1)y = \sin(2\log x)$$
 (06 Marks)

b. Solve
$$x^2p^2 + 3xyp + 2y^2 = 0$$
 (07 Marks)

c. Find the general and singular solution of Clairaut's equation
$$y = xp + p^2$$
. (07 Marks)

4 a. Solve
$$(2x + 1)^2 y'' - 2(2x + 1) y' - 12y = 6x$$
.
b. Solve $p^2 + 2py \cot x - y^2 = 0$. (07 Marks)

b. Solve
$$p^2 + 2py \cot x - y^2 = 0$$
. (07 Marks)

c. Find the general solution of
$$(p-1)e^{3x} + p^3 e^{2y} = 0$$
 by using the substitution $X = e^x$, $Y = e^y$.

(07 Marks)

5 a. Find the partial differential equation of all spheres
$$(x-a)^2 + (y-b)^2 + z^2 = c^2$$
. (06 Marks)

b. Solve
$$\frac{\partial^2 z}{\partial x \partial y} = \sin x \sin y$$
 for which $\frac{\partial z}{\partial y} = -2 \sin y$ when $x = 0$ and $z = 0$ when y is an odd

multiple of
$$\frac{\pi}{2}$$
. (07 Marks)

- a. Form the partial differential equation by eliminating the arbitrary function from $z = y\phi(x) + x\psi(y)$. (06 Marks)
 - b. Solve $\frac{\partial^2 z}{\partial y^2} = z$; given that when y = 0, $z = e^x$ and $\frac{\partial z}{\partial y} = e^{-x}$. (07 Marks)
 - c. Find the various possible solution for one dimensional heat equation by the method of separation of variables. (07 Marks)

Module-4

- a. Evaluate $\iint r \sin \theta \, dr \, d\theta$ over the cardioids $r = a(1 \cos \theta)$ above the initial line. (06 Marks)
 - b. Evaluate $\iiint x dz dx dy$. (07 Marks)
 - c. Derive the relation between Beta and Gamma function as $B(m,n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$.

OR

- Evaluate by changing the order of integration $\iint_{V}^{\infty} \frac{e^{-y}}{v} dy dx$. (06 Marks)
 - b. Find by double integration, the area lying between the parabola $y = 4x x^2$ and the line y = x. (07 Marks)
 - c. Show that $\int_{0}^{\pi/2} \sqrt{\cot \theta} \ d\theta = \frac{1}{2} \left[\left(\frac{1}{4} \right) \right] \left(\frac{3}{4} \right).$ (07 Marks)

- a. Find the Laplace transform of $\left[\frac{\text{Cosat} \text{Cosbt}}{t}\right]$ (06 Marks)
 - b. Express the function $f(t) = \begin{cases} Sint & 0 < t \le \frac{\pi}{2} \\ Cost & t > \frac{\pi}{2} \end{cases}$ in terms of unit step function and hence find

Laplace transform. (07 Marks)

c. Find $L^{-1} \left(\frac{s+2}{s^2 - 2s + 5} \right) \int_0^{\pi/2} \sqrt{\cot \theta} d\theta = \frac{1}{2} \left(\frac{1}{4} \right) \left(\frac{3}{4} \right)$ (07 Marks)

- Find the Laplace transform of the periodic function $f(t) = t^2$, 0 < t < 2. (06 Marks)
 - b. Using convolution theorem obtain the Inverse Laplace transform of $\frac{1}{s^3(s^2+1)}$. (07 Marks)
 - Solve by using Laplace transform $y'' + 4y' + 4y = e^{-t}$. Given that y(0) = 0, y'(0) = 0(07 Marks)