

18EE63

Sixth Semester B.E. Degree Examination, June/July 2024 **Digital Signal Processing**

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- Calculate 8-point DFT of $x(n) = \cos\left(\frac{n\pi}{4}\right)$. Draw magnitude and phase of x(k). (10 Marks) 1 a.
 - Derive the DFT properties for Periodicity and linearity property. b.

(10 Marks)

- Compute circular convolution of discrete sequence 2
 - $x_1(n) = \{1, 3, 5, 3\}$ $x_2(n) = \{2, 3, 1, 1\}$ by i) Circular method ii) Matrix method. (10 Marks)
 - Find the output y(n) of a filter whose impulse response is $h(n) = \{1, 1, 1\}$ and the input signal to the filter is $x(n) = \{3, -1, 0, 1, 3, 2, 0, 1, 2, 1\}$. Using overlap save method. (10 Marks)

Module-2

- Develop an 8-point DIF-FFT algorithm starting from DFT. State clearly all the step. 3 Explain how it reduces the number of computation. (10 Marks)
 - Find DFT of $x(n) = \{1, 1, 1, 1, 0, 0, 0, 0\}$ using DIT FFT algorithm show all the intermediate result in signal flow graph. (10 Marks)

OR

- The DFT x(k) of sequence is given as $x(k) = \{0, 2, +2j, -j4, 2-j2, 0, 2+2j, j4, 2-j2\}$ using using IDIF - FFT. Determine x(n).
 - Develop an 8-point IDIT-FFT algorithm starting from DFT. Draw the complete signal flow graph to find x(n).

Module-3

- Design an analog Butterfly filter has a gain 2dB and 20r/s and attenuation in excess of 10dB beyond 30r/s. (10 Marks)
 - Determine the transfer function if Chebyshev filter for the following specification:
 - i) Maximum passband repple is 1dB
 - Stop and band attenuation is 40dB for $\Omega \ge 4r/s$.

(10 Marks)

For the constraints $0.8 \le |H(e^{jw})| \le |$ for $0 \le w \le 0.2\pi$, $|H(e^{jw})| \le 0.2$ for $0.6\pi \le w \le \pi$. Design a Butterworth digital filter using bilinear transformation. Assume T = 1 Second.

Using Impulse invariant technique find the transfer function of digital filter H(z) for analog Transform function

$$H(s) = \frac{b}{(s+a)^2 + b^2}$$
.

(10 Marks)

Module-4

a. Design a Chebyshev filter with T = 1 second using Bilinear transformation for the following specification.

 $i) \quad 0.8 \leq |H(e^{jw})| \leq 1 \ \text{for} \ 0 \leq w \leq 0.2\pi$

(10 Marks)

ii) $|H(e^{jw})| \le 0.1$ for $0.5\pi \le w \le \pi$

b. Realise the system for direct Form – I and direct form – II.

 $H(z) = \frac{0.7 - 0.25z^{-1} - z^{-2}}{1 + 0.1z^{-1} - 0.72z^{-2}}$ (10 Marks)

- Obtain the parallel form and cascade form for given system. y(n) = 0.75 y(n-1) - 0.125y(n-2) + 6 x(n) + 7x(n-1) + x(n-2)(10 Marks)
 - b. Design a maximally flat digital LPF to meet following specification.

 $0.8 \le |H(e^{jw})| \le 1 \text{ for } 0 \le w \le \pi/4$

 $|H(e^{jw})| \le 0.18 \text{ for } 0.75\pi \le w \le \pi$

Using impulse invariant transformation. Assume T = 1 Sec.

(10 Marks)

- For a given FIR filter $y(n) = x(n) + \frac{\text{Module-5}}{2/5 x(n-1)} + \frac{3}{4x(n-2)} + .$ Draw direct form I and
 - Design the symmetric FIR lowpass filter whose desired frequency response is given as

 $H_{d}(w) = \begin{cases} e^{-jwz} & \text{for } |w| \le w_{c} \\ 0 & \text{otherwise} \end{cases}$

The length of the filter should be 7 and $w_c = 1$ radius/sample use rectangular window.

(10 Marks)

Determine the filter coefficient $h_d(n)$ for the desired frequency response of a low pass filter given by

 $H_{d}(e^{jw}) = \begin{cases} e^{-j2w} & \text{for } -\frac{\pi}{4} \le w \le \frac{\pi}{4} \\ 0 & \text{for } \frac{\pi}{4} \le |w| \le \pi \end{cases}$

If we define the new filter coefficient by $h(n) = h_d(n) \cdot w(n)$ where

 $w(n) = \begin{cases} 1 & \text{for } 0 \le n \le 4 \\ 0 & \text{for otherwise} \end{cases}$

Determine h(n) and also the necessary response |H(e^{jw})| and compare with |H_d (e^{jw})| determine H(ejw) Determine H(ejw) using Hamming window.

Determine form structures of casecade first order section also as a cascade 1st and 2nd order section form FIR lattice filter for $H(z) = |(1 + 0.6z^{-1})^5$.