

17EE45

Fourth Semester B.E. Degree Examination, Dec.2023/Jan.2024 Electromagnetic Field Theory

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

# Module-1

- a. Define scalar and vector. Two points A(2, 2, 1) and B(3, -4, 2) are given in the Cartesian system obtain the vector from A to B and a unit vector directed from A to B. (06 Marks)
  - b. Define divergence of a vector. What do positive and negative divergences represent.

(04 Marks)

c. Derive the relationship between cylindrical and spherical coordinate systems. (10 Marks)

#### OR

- 2 a. State and explain coulomb's law of force between the two point charges. (05 Marks)
  - b. Define electric field intensity (E). Find an expression for electric field intensity due to N different point charges. (07 Marks)
  - c. State and explain Gauss law in electrostatics. (08 Marks)

## Module-2

- 3 a. Define the following:
  - i) Potential difference and potential
  - ii) Potential gradient.

(06 Marks)

- b. Show that energy density in the electrostatic field is given by  $\frac{1}{2} \vec{D} \cdot \vec{E} J/m^3$ . (08 Marks)
- c. Given that the potential field is  $V = 2x^2y 5z$ . Find the potential, electric field intensity and volume charge density at point P(-4, 3, 6). (06 Marks)

#### OR

- 4 a. With necessary relations, define current and current density. (04 Marks)
  - b. Explain the boundary conditions for a boundary between two di-electric materials. (08 Marks)
  - c. Derive an expression for the capacitance per unit length of a two wire transmission line.

(08 Marks)

## Module-3

- 5 a. Derive Poisson's and Laplace equations starting from point form of Gauss law. (07 Marks)
  - b. Verify that the potential field given below satisfies the Laplace's equation:

 $V = 2x^2 - 3y^2 + z^2$ . (06 Marks)

c. State and prove Uniqueness Theorem. (07 Marks)

### OR

- 6 a. State and explain Biot-Savart's law. (07 Marks)
  b. State and explain Stoke's theorem. (06 Marks)
  - c. Derive an expression for vector magnetic potential. (07 Marks)

Module-4

- 7 a. Derive an expression for the force between differential current elements. (10 Marks)
  - b. A point charge of Q = -1.2C has velocity  $v = (5\bar{a}_x + 2\bar{a}_y 3\bar{a}_z)$  m/s. Find the magnitude of the force exerted on the charge if,
    - i)  $\bar{E} = -18\bar{a}_x + 5\bar{a}_y 10\bar{a}_z \text{ v/m}$
    - ii)  $\bar{B} = -4\bar{a}_x + 4\bar{a}_y 3\bar{a}_z T$
    - iii) Both are present simultaneously.

(10 Marks)

OR

- 8 a. Derive the boundary conditions at the interface between two magnetic materials of different permeabilities. (10 Marks)
  - b. Calculate the inductance of a solenoid of 200 turns wound tightly on a cylindrical tube of 6cm diameter. The length of the tube is 60cm and the solenoid is in air. (03 Marks)
  - c. Define mutual inductance. Derive an expression for mutual inductance of two different coils.

    (07 Marks)

Module-5

- 9 a. Explain briefly Faraday's law and displacement current for time varying fields. (08 Marks)
  - b. In a given lossy dielectric medium, conduction current density  $J_C = 0.02 \sin 10t \, (A/m^2)$ . Find the displacement current density if  $\sigma = 10^3 \text{s/m}$  and  $\varepsilon_r = 6.5$ . (05 Marks)
  - c. Write Maxwell's equations in point form and in integral from for time varying fields.

(07 Marks)

OR

- 10 a. Discuss the propagation of uniform plane waves in a lossless medium. (07 Marks)
  - b. Define poynting vector and explain the power flow associated with it. (07 Ma
  - c. A 300MHz uniform plane wave propagates through fresh water for which  $\sigma = 0$ ,  $\mu_r = 1$  and  $\epsilon_r = 78$ . Calculate:
    - i) The attenuation constant
    - ii) The phase constant
    - iii) The wave length.

(06 Marks)