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18EC55

## Fifth Semester B.E. Degree Examination, June/July 2023 Electromagnetic Waves

Time: 3 hrs.

Max. Marks: 100

*Note: Answer any FIVE full questions, choosing ONE full question from each module.*

### Module-1

- 1 a. Derive the expression for Electric Field due to line charge of infinite length. (08 Marks)
- b. Find the force on  $100 \mu\text{C}$  charge at  $(0, 0, 3)\text{m}$ , if four like charges of  $20 \mu\text{C}$  are located on the x and y axis at  $\pm 4\text{m}$ . (06 Marks)
- c. Determine Electric Field at origin due to charge at  $6.44 \times 10^{-9}\text{C}$  located at  $(4, 2, -3)\text{m}$  in Cartesian coordinate system. (06 Marks)

OR

- 2 a. A charge lies in the  $Z = -3\text{m}$  plane in the form of a square sheet defined by  $-2 \leq x \leq 2, -2 \leq y \leq 2\text{m}$  with  $\rho_s = 2(x^2 + y^2 + 9)^{3/2}\text{nc}$ . Find Electric field at origin. (07 Marks)
- b. Three negative charges  $Q_1 = -1 \mu\text{C}, Q_2 = -2 \mu\text{C}, Q_3 = -3 \mu\text{C}$  are placed at the corners of an equilateral triangle. If length of each side is  $1\text{m}$ , find magnitude and direction of EF at a point bisecting line between the charge  $Q_2$  and  $Q_3$ . (08 Marks)
- c. Derive the expression for Electric field intensity due to several point charges. (05 Marks)

### Module-2

- 3 a. A charge  $Q$  is uniformly distributed in a square ring of side  $l$ . Find  $E$  and  $V$  at centre of the ring. (08 Marks)
- b. Determine work done in carrying a charge of  $-2\text{C}$  from  $(2, 1, -1)$  to  $(8, 2, -1)$  in Electric field  $E = y\hat{a}_x + x\hat{a}_y$  considering the path along parabola  $x = 2y^2$ . (05 Marks)
- c. State and prove Gauss divergence theorem. (07 Marks)

OR

- 4 a. A point charge  $Q = 90 \mu\text{C}$  is located at origin and these are two uniformly surface charge density distribution  $-8 \mu\text{C}/\text{m}^2$  at  $r = 1\text{m}$  and  $4.5 \mu\text{C}/\text{m}^2$  at  $r = 2$ . Find  $\vec{D}$  everywhere. (08 Marks)
- b. Given  $D = 5r \hat{a}_r \text{C}/\text{m}^2$ . Determine whether divergence theorem holds good for shell region enclosed by spherical surface at  $r = a$  and  $r = b (b > a)$  centred at origin. (07 Marks)
- c. Find the potential and volume charge density at  $P(0.5, 1.5, 1)\text{m}$  in free space given  $V = 2x^2 - y^2 - z^2$ . (05 Marks)

### Module-3

- 5 a. Let  $V = A \ln \left[ \frac{B(1 - \cos \theta)}{1 + \cos \theta} \right]$ 
  - i) Show that  $V$  satisfies Laplace equation in spherical coordinates.
  - ii) Find  $A$  and  $B$ , so that  $V = 100\text{V}$  and  $E = 500$  at  $r = 5\text{cm}, \theta = 90^\circ, \phi = 60^\circ$ . (08 Marks)
- b. State and explain Stokes theorem. (04 Marks)
- c. Determine whether or not the following potential satisfy Laplace equation :
  - i)  $V = r \cos \phi + z$
  - ii)  $V = x^2 - y^2 + z^2$  (08 Marks)

OR

- 6 a. Find the magnetic field intensity at P for the Fig.Q6(a).

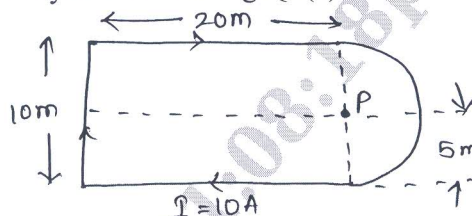


Fig.Q6(a)

- (08 Marks)
- b. There exist a potential of  $V = -2.5V$  on the conductor of  $0.02m$  and  $V = 15V$  at  $r = 0.35m$ . Determine  $E$  and  $D$  by solving Laplace equation in spherical coordinates. (07 Marks)
- c. If the magnetic field intensity in region  $H = (3y - 2)\hat{a}_z + 2x\hat{a}_y$ . Find current density. (05 Marks)

**Module-4**

- 7 a. For region1,  $\mu_1 = 4\mu$  H/m and for region2,  $\mu_2 = 6\mu$  H/m. The regions are separated by  $Z = 0$  plane. The surface current density at the boundary is  $K = 100\hat{a}_x$  A/m. Find  $B_2$  if  $B_1 = 2\hat{a}_x - 3\hat{a}_y + \hat{a}_z$  mT for  $Z = 0$ . (08 Marks)
- b. A circular conducting loop of radius  $40cm$  lies in  $xy$  plane and has a resistance of  $20\Omega$ . If magnetic flux density is  $B = 0.2 \cos(500t)\hat{a}_x + 0.75\sin(400t)\hat{a}_y + 1.2\cos(314t)\hat{a}_z$ . Find induced current in Loop. (07 Marks)
- c. Explain Lorentz force equation. (05 Marks)

OR

- 8 a. A conductor of length  $2.5m$  in  $Z = 0$  and  $x = 4m$  carries a current of  $12A$  in  $-\hat{a}_y$  direction. Calculate uniform flux density in region, if force on the conductor is  $12 \times 10^{-2} N$  in direction by  $\left[ \frac{-\hat{a}_x + \hat{a}_z}{\sqrt{2}} \right]$ . (07 Marks)
- b. Explain Magnetization and Permeability. (07 Marks)
- c. Explain force between differential current elements with equation. (06 Marks)

**Module-5**

- 9 a. Given  $H = H_m e^{j(\omega t + \beta z)} \hat{a}_x$  A/m in free space. Find  $E$ . (07 Marks)
- b. Derive the wave equation for vector  $E$  and  $H$  field in conducting medium. (08 Marks)
- c. Prove that  $\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$ . (05 Marks)

OR

- 10 a. Discuss the propagation of uniform plane wave in good conductor and explain skin depth. (08 Marks)
- b. Determine  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $v$ ,  $\lambda$ ,  $\eta$  for damp soil at frequency of  $1 MHz$  given that  $\epsilon_r = 12$ ,  $\mu_r = 1$ , and  $\sigma = 20m S/m$ . (05 Marks)
- c. Find the Amplitude of displacement current density in free space within large power distribution  
 $H = 10^6 \cos(377t + 1.256 \times 10^{-6}z)\hat{a}_y$  (07 Marks)

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