

# CBCS SCHEME

17EC42

## Fourth Semester B.E. Degree Examination, June/July 2023 Signals and Systems

Time: 3 hrs.

Max. Marks: 100

*Note: Answer any FIVE full questions, choosing ONE full question from each module.*

### Module-1

- 1 a. Check for periodicity and find its time period for the signal  $x(n) = \cos \frac{\pi}{2}n \cdot \cos \frac{\pi}{3}n$ . (07 Marks)
- b. Calculate energy or power for the signal  $x(t)$  given in Fig.Q1(b).

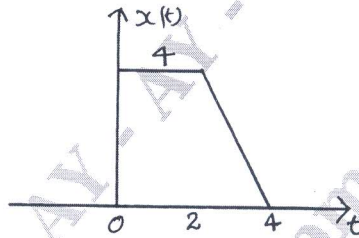


Fig.Q1(b)

- c. Given that  $x(n) = \{2, 3, 4, 6\}$ , sketch  $x(-2n + 1)$ . (06 Marks)

**OR**

- 2 a. Represent the signal  $x(t)$  in terms of  $g(t)$  given in the Fig.Q2(a).

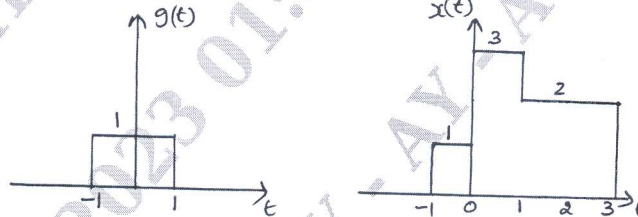


Fig.Q2(a)

- b. Given that signal  $x(n) = 2n[u(n-1) - u(n-7)]$ . Sketch the signals  $x(2n-3)$  and  $x(n+4)$ . (06 Marks)
- c. Check for Linearity and Time invariance for the given system equation:

$$y(t) = x(t) + \frac{1}{x(t-1)}$$

(06 Marks)

### Module-2

- 3 a. Given that
  - $x(t) = e^{-at}$  for  $0$  to  $T$
  - $h(t) = 1$  for  $0$  to  $2T$
 Calculate  $y(t) = x(t) * h(t)$  (10 Marks)
- b. Prove the following properties of convolution in continuous domain:
  - (i) Associative (10 Marks)
  - (ii) Commutative

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

OR

- 4 a. Given that  $x(t) = 3U(t) - 3U(t - 4)$ ,  $h(t) = 2\delta(t - 1) + \delta(t - 3)$ . Calculate  $y(t) = x(t) * h(t)$  using properties. (10 Marks)
- b. Given that
- $$x(n) = \alpha^n \quad 2 \leq n \leq 6 \quad \text{for } 0 < \alpha < 1$$
- $$h(n) = 1 \quad 0 \leq n \leq 4$$
- Find  $y(n) = x(n) * h(n)$  by proper graphs. (10 Marks)

**Module-3**

- 5 a. Find step response for the given impulse response
- (i)  $h(t) = e^{-at} U(t - 2)$
- (ii)  $h(n) = \left(\frac{1}{2}\right)^n U(n - 3)$
- (iii)  $h(t) = t U(t)$  (09 Marks)
- b. Derive the formula to calculate step response in terms of impulse response. (05 Marks)
- c. Find CTFS coefficient for the signal  $x(t) = \sin 2\pi t + \cos 3\pi t$ . (06 Marks)

OR

- 6 a. Define the causality for impulse response representation of the system and check the same for the following:
- (i)  $h(t) = e^t U(t - 2)$
- (ii)  $h(n) = a^n U(n + 3) \quad 0 < a < 1$  (06 Marks)
- b. Find FS for the signal  $x(t)$  in Fig.Q6(b). Also calculate magnitude and phase angle.

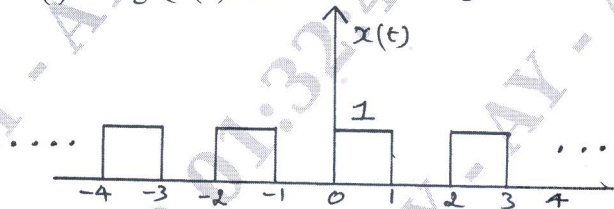


Fig.Q6(b)

- (09 Marks)
- c. Find DTFS coefficient for the signal  $x(n) = \cos\left(\frac{2\pi}{3}n + \frac{\pi}{3}\right)$ . (05 Marks)

**Module-4**

- 7 a. Find DTFT for the following signal using appropriate properties:
- (i)  $x(n) = e^{-j2n} (3)^n U(n)$
- (ii)  $x(n) = 2^n U(n - 1)$  (10 Marks)
- b. Find IFT for the spectrum  $X(j\omega) = \frac{-j\omega}{(j\omega)^2 + 3(j\omega) + 2}$ . (10 Marks)

OR

- 8 a. Find IDTFT for the spectrum using convolution property
- $$X(e^{j\Omega}) = \frac{1}{(1 - ae^{-j\Omega})^2}$$
- (10 Marks)
- b. Find FT of the signal  $x(t) = e^{-at} U(t)$  and calculate magnitude and phase angle. (10 Marks)

**Module-5**

- 9 a. Give all ROC properties of Z-transform. (05 Marks)  
 b. Find z-transform for the signal and plot ROC  $x(n) = (n-2)(3)^{n-2}U(n-2)$ . (06 Marks)  
 c. Find Inverse Z-transform using partial fraction method:

$$X(z) = \frac{1 - z^{-1} + z^{-2}}{\left(1 - \frac{1}{2}z^{-1}\right)(1 - 2z^{-1})(1 - z^{-1})}$$

for the ROC  $1 < |z| < 2$

(09 Marks)

**OR**

- 10 a. Find transfer function and impulse response for the causal system for the given input and output signals:

$$x(n) = \left(-\frac{1}{3}\right)^n U(n); \quad y(n) = 3(-1)^n U(n) + \left(\frac{1}{3}\right)^n U(n) \quad (10 \text{ Marks})$$

- b. Find z-transform and plot ROC with poles and zeros for the given signal

$$x(n) = (2)^n U(n) + (-3)^n U(-n) \quad (10 \text{ Marks})$$

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