

CBCS SCHEME



USN

BMATE101

First Semester B.E./B.Tech. Degree Examination, Jan./Feb. 2023

Mathematics - I for Electrical and Electronics Engineering Stream

Time: 3 hrs.

Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.

2. VTU Formula Hand Book is permitted.

3. M : Marks , L: Bloom's level , C: Course outcomes.

Module – 1			M	L	C
Q.1	a.	If ϕ is the angle between the radius vector and tangent to the polar curve $r = t(\theta)$, prove that $\tan \phi = r \frac{d\theta}{dr}$.	6	L2	CO1
	b.	Find the angle between the curves $r = \sin \theta + \cos \theta$ and $r = 2 \sin \theta$.	7	L2	CO1
	c.	Find the radius of curvature of the curve $x^3 + y^3 = 3axy$ at $\left(\frac{3a}{2}, \frac{3a}{2}\right)$.	7	L2	CO1

OR

Q.2	a.	Prove that the polar curves $r = a(1 + \cos \theta)$ and $r = b(1 - \cos \theta)$ intersect orthogonally.	6	L2	CO1
	b.	Find the radius of curvature of the curve $y = 4 \sin x - \sin 2x$ at $x = \frac{\pi}{2}$.	7	L2	CO1
	c.	Using Modern mathematical tool, write a program / code to plot the curve $r = 2 \cos 2\theta $.	7	L3	CO5

Module – 2

Q.3	a.	Expand $f(x) = \cos x + \sin x$ in a Maclaurin series upto the term involving x^5 .	6	L2	CO2
	b.	If $U = \log(\tan x + \tan y + \tan z)$, show that $\sin 2x \frac{\partial U}{\partial x} + \sin 2y \frac{\partial U}{\partial y} + \sin 2z \frac{\partial U}{\partial z} = 2$.	7	L2	CO2
	c.	If $u = x^2 + y^2 + z^2$, $v = xy + yz + zx$, $w = x + y + z$, find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$.	7	L2	CO2

OR

Q.4	a.	Evaluate $\lim_{x \rightarrow 0} \left(\frac{a^x + b^x + c^x + d^x}{4} \right)^{\frac{1}{x}}$.	6	L1	CO2
	b.	If $V = f(x-y, y-z, z-x)$, show that $\frac{\partial V}{\partial x} + \frac{\partial V}{\partial y} + \frac{\partial V}{\partial z} = 0$.	7	L2	CO2
	c.	Using modern mathematics tool, write a program / code to show that $U_{xx} + U_{yy} = 0$. Given $U_3 = e^x (x \cos y - y \sin y)$.	7	L3	CO2

Module - 3

Q.5	a.	Solve $(5x^4 + 3x^2y^2 - 2xy^3) dx + (2x^3y - 3x^2y^2 - 5y^4) dy = 0$.	6	L2	CO3
	b.	Find the Orthogonal trajectory of the family of confocal ellipses $\frac{x^2}{a^2} + \frac{y^2}{b^2 + \lambda} = 1$, where λ is a parameter.	7	L3	CO3
	c.	Solve $xyp^2 - (x^2 + y^2)p + xy = 0$.	7	L2	CO3

OR

Q.6	a.	Solve $\frac{dy}{dx} + y \tan x = y^2 \sec x$.	6	L2	CO3
	b.	Find the current i at any time t , if initially there is no current in the circuit governed by the differential equation $L\left(\frac{di}{dt}\right) + Ri = 200 \sin 300t$, when $L = 0.05$ and $R = 100$.	7	L3	CO3
	c.	Find the general solution of the equation $(px - y)(py + x) = a^2 p$ by reducing into Clairaut's form, taking the substitution $X = x^2$, $Y = y^2$.	7	L2	CO3

Module - 4

Q.7	a.	Evaluate $\int_0^1 \int_x^{\sqrt{x}} xy \, dy \, dx$, by changing the order of integration.	6	L2	CO4
	b.	Evaluate $\int_{-p}^1 \int_0^z \int_{x-z}^{x+z} (x + y + z) \, dy \, dx \, dz$.	7	L2	CO4
	c.	Prove that $\beta(m, n) = \frac{\Gamma(m)(n)}{\Gamma(m+n)}$.	7	L1	CO4

OR

Q.8	a.	Evaluate $\int_0^1 \int_0^{\sqrt{1-y^2}} (x^2 + y^2) \, dx \, dy$ by changing to polar coordinates.	6	L2	CO4
	b.	Using double integration, find the area bounded by the parabolas $y^2 = 4ax$ and $x^2 = 4ay$.	7	L3	CO4
	c.	Show that $\int_0^{\pi/2} \sqrt{\sin \theta} \, d\theta \times \int_0^{\pi/2} \frac{d\theta}{\sqrt{\sin \theta}} = \pi$ by using Beta and Gamma functions.	7	L2	CO4

Module - 5

Q.9	a.	Find the rank of the matrix $\begin{bmatrix} 2 & 1 & 3 & 5 \\ 4 & 2 & 1 & 3 \\ 8 & 4 & 7 & 13 \\ 8 & 4 & -3 & -1 \end{bmatrix}$	6	L2	CO5
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	b.	Solve the system of linear equations by Gauss – Jordan method. $x + y + z = 11$ $3x - y + 2z = 12$ $2x + y - z = 3.$	7	L2	CO5
	c.	Determine the largest eigen value and the corresponding eigen vector of the matrix. $A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$ by using Power method with initial eigen vector $X_0 = [1 \ 0 \ 0]^T$. Carry out six iterations.	7	L2	CO5
OR					
Q.10	a.	For what values of λ and μ the system of equations $x + y + z = 6$, $x + 2y + 3z = 10$ and $x + 2y + \lambda z = \mu$ may have i) Unique solution ii) Infinite number of solution iii) No solution.	6	L2	CO5
	b.	Solve by using Gauss elimination method the equations $3x + y - z = 3$; $2x - 8y + z = -5$; $x - 2y + 9z = 8.$	7	L2	CO5
	c.	Using modern mathematical tool, write a program / code to find the largest eigen value of $A = \begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{bmatrix}$ by power method.	7	L3	CO5
