

USN

Fifth Semester B.E. Degree Examination, Jan./Feb. 2023 Information Theory and Coding

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Explain the terms:
 - i) Self Information
 - ii) Average Information
 - iii) Mutual Information
 - iv) Efficiency
 - v) Redundancy. (10 Marks)
- b. Write the block diagram of digital communication system and explain. (10 Marks)

OR

- 2 a. What is Entropy? Explain properties of entropy. (10 Marks)
- b. In a binary PCM, if '0' occur with probability 1/4 and '1' occur with probability 3/4, then calculate amount of information conveyed by each bit. (10 Marks)

Module-2

- 3 a. Explain KRAFT INEQUALITY theorem. (10 Marks)
- b. Explain Shannon's encoding algorithm. (10 Marks)

OR

- 4 a. Apply Shannon's encoding algorithm to the following messages $\{S_1, S_2, S_3\}$ with probabilities $\{0.5, 0.3, 0.2\}$ to find code-words and also find code-efficiency and redundancy. (10 Marks)
- b. Explain properties of codes. (10 Marks)

Module-3

- 5 a. Consider a binary channel shown in Fig.Q.5(a) given below.

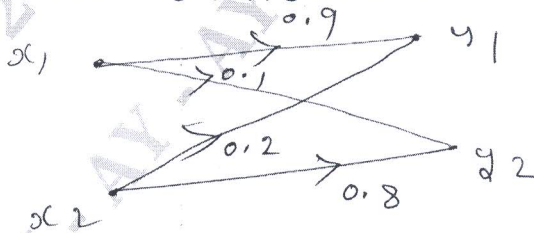


Fig.Q.5(a)

- i) Find the channel matrix of the channel.
- ii) Find $P(y_1)$ and $P(y_2)$ when $P(x_1) = P(x_2) = 0.5$.
- iii) Find the joint probabilities $P(x_1, y_2)$ and $P(x_2, y_1)$ when $P(x_1) = P(x_2) = 0.5$. (10 Marks)
- b. For a noiseless channel with an input symbols and m output symbols. Prove that $H(X) = H(Y)$ and $H(Y/X) = 0$. (10 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

OR

- 6 a. State and discuss Shannon's theorem on channel capacity. (10 Marks)
 b. A binary channel has the following characteristics:

$$P(Y/X) = \begin{bmatrix} 2/3 & 1/3 \\ 1/3 & 2/3 \end{bmatrix}$$

If input symbols are transmitted with probabilities $3/4$ and $1/4$ respectively, find entropies $H(X)$, $H(X, Y)$ and $H(Y/X)$. (10 Marks)

Module-4

- 7 a. With a neat block diagram and a suitable example, explain the error-control based communication system. (10 Marks)
 b. Distinguish between "block codes" and "convolutional codes". (10 Marks)

OR

- 8 Consider a (6, 3) linear code whose generator matrix is

$$G = \begin{bmatrix} 1 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

- i) Find all code vectors.
 ii) Find all Hamming weights and distances.
 iii) Find minimum weight parity check matrix.
 iv) Draw the encoder circuit for the above codes. (20 Marks)

Module-5

- 9 a. Write a note on: i) Golay codes ii) BCH codes. (10 Marks)
 b. Discuss the various properties of cyclic codes. (10 Marks)

OR

- 10 Explain encoding of convolution codes using transform-domain approach, with an examples. (20 Marks)
