

# GBGS SCHEME

17EE54

# Fifth Semester B.E. Degree Examination, Jan./Feb. 2023 Signals and Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

# Module-1

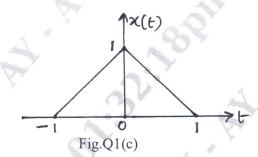
- 1 a. Distinguish between:
  - i) Continuous and discrete time signals
  - ii) Even and odd signals
  - iii) Periodic and non-periodic signals
  - iv) Power and energy signals.

(08 Marks)

b. Find the even and odd components of the signal  $x(t) - e^{-2t} \cos t$ .

(04 Marks)

- c. A triangular pulse signal x(t) is depicted in Fig.Q1(c). Sketch each of the following signals derived from x(t).
  - i) x(3t)
  - ii) x(3t+2)
  - iii) x(2(t+2))
  - iv) x(3t) + x(3t + 2)



(08 Marks)

OR

- 2 a. For each of the following signals, determine whether it is periodic, and if it is, find the fundamental period: i)  $x(t) = \sin^3(2t)$  ii)  $x[n] = [-1]^{n^2}$  iii)  $x[n] = \cos[2n]$ . (06 Marks)
  - b. Categorize each of the following signals as an energy signal or a power signal and find its corresponding value.

i) 
$$x(t) = \begin{cases} t; & 0 \le t \le 1 \\ 2 - t; & 1 \le t \le 2 \\ 0; & \text{otherwise} \end{cases}$$

$$ii) x(n) = \begin{cases} n; & 0 \le n \le 5 \\ 10 - n; & 5 \le n \le 10 \\ 0; & otherwise \end{cases}$$

(06 Marks)

- c. Check whether the following system is:
  - i) Static or dynamic
  - ii) Linear or non linear
  - iii) Causal or non-causal
  - iv) Time invariant or time variant Justify the answer.  $y[n] = log_{10} |x[n]|$ .

(08 Marks)

## Module-2

3 a. Find the convolution sum of the sequences:

$$x[n] = \{3, 4, 1, 2\} \text{ and } h[n] = \{1, 1, 2, 3\}$$

using graphical method.

(08 Marks)

(06 Marks)

- b. For the following impulse responses, determine whether the corresponding system is memoryless; causal and stable. Justify the answer:
  - i)  $h(t) = e^{at}u(t); a < 0$

ii) 
$$h[n] = \left[\frac{1}{2}\right]^n u[n]$$
.

c. Draw direct form I and direct form II implementations of the system described by the difference equation:  $y[n] + \frac{1}{4}y[n-1] + \frac{1}{8}y[n-2] = x[n] + x[n-1]$ . (06 Marks)

### OR

4 a. Evaluate the convolution integral for a system with input x(t) and impulse response h(t), given by:

$$x(t) = \begin{cases} 1, & 0 < t < 2 \\ 0, & \text{otherwise} \end{cases} \quad h(t) = e^{-t}u(t). \tag{08 Marks}$$

b. Find the step response of the first – order recursive system with impulse response.

 $h[n] = \alpha^n u[n]$ , assuming that  $|\alpha| < 1$ . (04 Marks) c. Find the complete solution for the first-order recursive system described by difference

Find the complete solution for the first-order recursive system described by difference equation:  $y[n] - \frac{1}{4}y[n-1] = x[n]$ , if input  $x[n] = \left[\frac{1}{2}\right]^n u(n)$  and the initial condition is y[-1] = 8.

#### Module-3

5 a. Find the Fourier transform of the following signals:

$$i) x(t) = e^{2t} u(-t)$$

ii) 
$$x(t) = e^{-|t|}$$
. (06 Marks)

- b. State and prove convolution property of continuous time Fourier transform. (08 Marks)
- c. Find the Fourier transform of the system output, for the following input and impulse response:  $x(t) = 3e^{-t}u(t)$  and  $h(t) = 2e^{-2t}u(t)$ . (06 Marks)

### OR

- 6 a. Prove differentiation in time property of CTFT. (06 Marks)
  - b. Determine the time-domain signal corresponding to the following Fourier transform.

$$X(j\omega) = \frac{-j\omega}{(j\omega)^2 + 3j\omega + 2}.$$
 (08 Marks)

c. Find the frequency response of LTI system described the differential equation:

$$\frac{d^{3}y(t)}{dt^{3}} + \frac{6d^{2}y(t)}{dt^{2}} + \frac{5dy(t)}{dt} + 4y(t) = 3x(t). \tag{06 Marks}$$