

15MT73

# Seventh Semester B.E. Degree Examination, July/August 2022 **Signal Process**

Fime: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

# Module-1

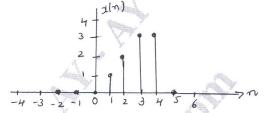
- Illustrate the following with examples each: 1
  - i) Even and odd signals
  - Energy and power signals ii)
  - Continuous and discrete signals.

Find the even and odd components of  $x(t) = e^{jt}$ .

(08 Marks)

b. A discrete time signal x(n) is shown in Fig.Q.1(b), sketch and label each of the following signals: i) x(n-2)ii) x(2n)iii) x(-n) (08 Marks)





# OR

- For a system described by  $T\{x(n)\} = ax(n) + b$  check for the following properties:

  - i) Stability ii) Causality
- iii) Linearity (iv) Time invariance
- v) Memory.
- (10 Marks) b. Determine whether each of the following signals is periodic. If a signal is periodic, find its fundamental period. i)  $x(n) = 5\cos(0.2\pi n)$ ii)  $x(n) = \sin(2n)$ . (06 Marks)

3 State and prove convolutional integral.

(08 Marks)

An LTI system is characterized by an impulse response:

$$h(n) = \left(\frac{3}{4}\right)^n u(n)$$

Find the step response of the system. Also evaluate the output of the system  $n = \pm 5$ .

(08 Marks)

State and prove the convolutional sum.

(08 Marks)

- Find the convolutional sum of two sequences  $x_1(n)$  and  $x_2(n)$  given below:

ii) 
$$x_2(n) = (2, 1, 4)$$

(08 Marks)

### Module-3

State the definition of Discrete Fourier Transform (DFT), compute the 8 point DFT of the 5 sequence x(n) given below:

$$x(n) = (1, 1, 1, 1, 0, 0, 0, 0).$$

(10 Marks)

b. Find the N point DFT of the following sequences:

i) 
$$x_1(n) = \delta(n)$$

ii) 
$$x_2(n) = \delta(n-n_0)$$

(06 Marks)

- 6 a. Explain the properties of DFT.
  - i) Linearity ii) Circular time shift. Find the 4 point DFT of the sequence x(n) = (1, -1, 1, -1). Also using time shift property find the DFT of the sequence  $y(n) = x((n-2))_4$ . (10 Marks)
  - b. Compute the 4 point DFT of sequence x(n) = (1, 0, 1, 0). Also find y(n) if  $y(k) = x((k-2))_4$ .

# Module-4

- 7 a. A Butterworth low pass filter has to meet the following specifications:
  - i) Passband gain,  $K_P = -1 dB$  at  $\Omega p = 4 rad/sec$ .
  - ii) Stop band attenuation greater than or equal to 20dB at  $\Omega_s$  = 8rad/sec.

Determine the transfer function Ha(s) of the lowest order Butterworth filter to meet the above specifications.

(10 Marks)

b. Find the order N of a low pass Butterworth filter to meet the following specifications:  $\delta_p = 0.001$ ,  $\delta_s = 0.001$ ,  $\Omega_p = 1 \text{rad/sec}$ ,  $\Omega_s = 2 \text{rad/sec}$ . (06 Marks)

### OR

- 8 a. Design a Chebyshev analog low pass filter that has a -3dB cutoff frequency of 100 rad/sec and a stop band attenuation of 25dB or greater for all radian frequencies past 250rad/sec.
  - b. Let  $Ha(s) = \frac{b}{(s+a)^2 + b^2}$  be a casual second order analog transfer function. Show that the

casual second order digital transfer function H(z) obtained from Ha(s) through impulse invariance method is given by

$$H(z) = \frac{e^{-aT} \sin bT z^{-1}}{1 - 2e^{-aT} \cos bT z^{-1} + e^{-2aT} z^{-2}}. \text{ Also find } H(z) \text{ when } Ha(s) = \frac{1}{s^2 + 2s + 2}. \quad \text{(06 Marks)}$$

# Module-5

9 a. The frequency response of an FIR filter is given by

 $H(W) = e^{-j3w}(1+1.8\cos 3w + 1.2\cos 2w + 0.5\cos w)$ 

Determine the coefficients of the impulse response h(n) of the FIR filter. (10 Marks)

b. Obtain a cascade realization for a system described by

$$H(z) = \frac{1 + \frac{1}{4}z^{-1}}{\left(1 + \frac{1}{2}z^{-1}\right)\left(1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2}\right)}.$$
 (06 Marks)

### OR

10 a. Draw the block diagram of direct form I and direct form II realization for a digital IIR filter described by the system function

$$H(z) = \frac{8z^3 - 4z^2 + 11z - 2}{\left(3 - \frac{1}{4}\right)\left(z^2 - z + \frac{1}{2}\right)}$$
 (10 Marks)

b. Obtain a parallel realization for the transfer function H(z) given below:

$$H(z) = \frac{8z^3 - 4z^2 + 11z - 2}{\left(z - \frac{1}{4}\right)\left(z^2 - z + \frac{1}{2}\right)}.$$
 (06 Marks)