

USN

--	--	--	--	--	--	--	--	--	--

15EC43

Fourth Semester B.E. Degree Examination, July/August 2022
Control Systems

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Define control system. What are the requirements of a good control system? (04 Marks)
 b. For the mechanical system shown in Fig.Q1(b).
 (i) Draw the mechanical network
 (ii) Write the differential equations
 (iii) Draw an electrical network based on Force-Voltage Analogy

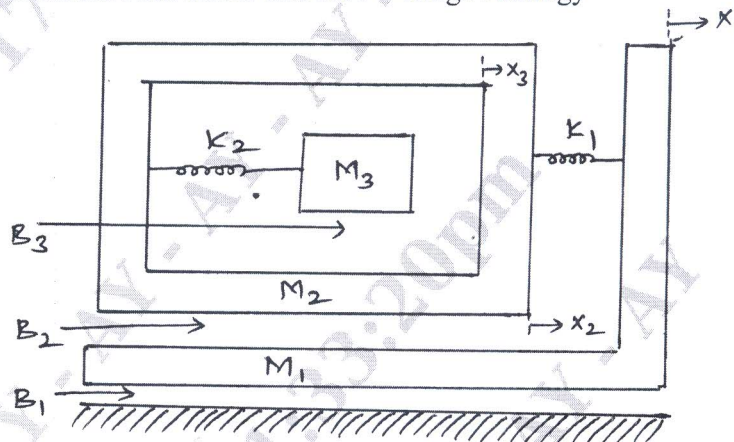


Fig.Q1(b)

(06 Marks)

- c. Draw the signal flow graph shown in Fig.Q1(c). Determine the transfer function using Mason's gain formulae.

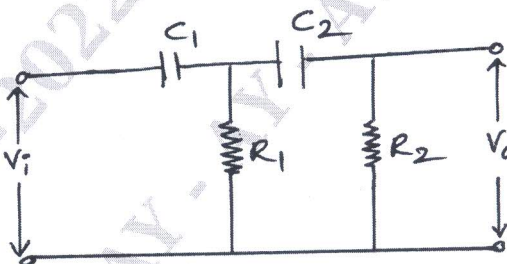


Fig.Q1(c)

(06 Marks)

OR

- 2 a. Define the following terms related to signal-flow graph with a neat schematic:
 (i) Forward path
 (ii) Feedback loop
 (iii) Self loop
 (iv) Source node

(04 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
 2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

- b. For the mechanical system shown in Fig.Q2(b).
 (i) Draw equivalent mechanical network.
 (ii) Write the performance equations.
 (iii) Draw torque-current analogy.

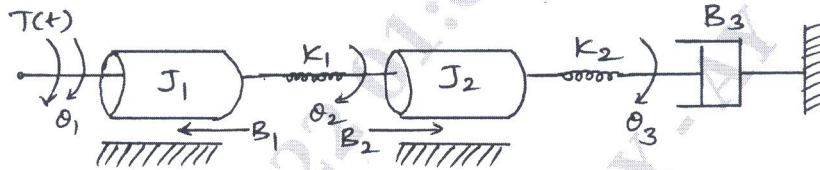


Fig.Q2(b)

(06 Marks)

- c. Obtain the transfer function of the control system whose block diagram is shown in Fig.Q2(c) using block diagram reduction techniques.

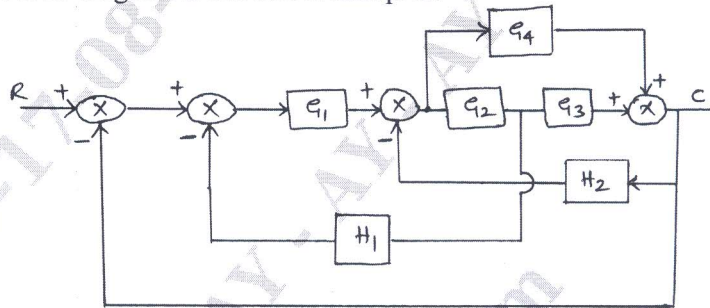


Fig.Q2(c)

(06 Marks)

Module-2

- 3 a. Draw the transient characteristics of a control system to a unit step input and define the following:
 (i) Delay time (ii) Rise time (iii) Peak time
 (iv) Settling time (v) Maximum overshoot

(06 Marks)

- b. A unity feedback control system has an open-loop transfer function $G(s) = \frac{5}{s(s+1)}$, find the rise time, percentage overshoot, peak time and settling time for a step input of 10 units.

(06 Marks)

- c. Determine the static error coefficients for a unity feedback system given by

$$G(s) = \frac{K}{s^2(s+20)(s+30)}$$

(04 Marks)

OR

- 4 a. The response of a serve mechanism is $c(t) = 1 + 0.2e^{-60t} - 1.2e^{-10t}$ when subjected to a unit step input. Obtain an expression for closed loop transfer function. Determine the undamped natural frequency and damping ratio.
 b. A second order control system is represented by a transfer function given below:

(04 Marks)

$$\frac{\theta_0(s)}{T(s)} = \frac{1}{Js^2 + Fs + K}$$

where $\theta_0(s)$ = proportional output; T = input torque. A step unit of 10 N-m is applied to the system and test results are given below:

- (i) Maximum overshoot is 6%.
 (ii) Peak time is 1 sec
 (iii) The steady state value of the output is 0.5 radian.

Determine the values of J, F and K.

(06 Marks)

- c. Find K_p , K_v and K_a for the unity feedback system represented by the following open loop transfer function $G(s) = \frac{100}{s^2(s+2)(s+5)}$. Determine the steady state error when input is $r(t) = 1 + t + 2t^2$. (06 Marks)

Module-3

- 5 a. For system $s^4 + 22s^3 + 10s^2 + s + K = 0$, find K_{mar} and ' ω ' at K_{mar} . (04 Marks)
 b. A given system shown in Fig.Q5(b) oscillates with frequency 2 rad/sec. Find the value of K_{mar} and P. No poles are in RHS.

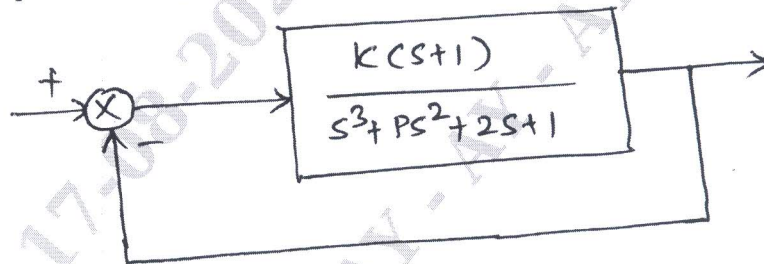


Fig.Q5(b)

- c. The open loop transfer function of control system is given by

$$G(s)H(s) = \frac{K(s+1)}{s(s-1)(s^2+5s+20)}$$

Determine the valid break away points.

- OR**
- 6 a. What are the necessary and sufficient conditions for a system to be stable according to Routh-Hurwitz criterion. (04 Marks)
 b. A feedback control system has open loop transfer function $G(s)H(s) = \frac{K}{s(s+4)(s^2+4s+20)}$. Plot complete root locus for $K = 0$ to ∞ . Indicate all the points on it. (10 Marks)
 c. Examine the stability of given equation using Routh's method $s^3 + 6s^2 + 11s + 6 = 0$. (02 Marks)

Module-4

- 7 a. Plot the polar plot for the transfer function given $G(s)H(s) = \frac{1}{s(Ts+1)}$. (06 Marks)
 b. For a certain control system $G(s)H(s) = \frac{K}{s(s+2)(s+10)}$. Sketch the Nyquist plot and hence calculate the range of value of ' K ' for stability. (10 Marks)

OR

- 8 a. List the limitations of lead and lag compensations. (06 Marks)
 b. A unity feedback control system has $G(s) = \frac{80}{s(s+2)(s+20)}$. Draw the Bode plot. Determine GM, PM, ω_{gc} and ω_{pc} . (10 Marks)

Module-5

- 9 a. Define the following terms:
 (i) State (ii) State variable (iii) State space (iv) State trajectory (04 Marks)
- b. Construct the state model using phase variables if the system is described by the differential equation

$$\frac{d^3y(t)}{dt^3} + 4\frac{d^2y(t)}{dt^2} + 7\frac{dy(t)}{dt} + 2y(t) = 5U(t)$$

where $y(t)$ = output; $U(t)$ = input to the system. Draw the state diagram. (06 Marks)

- c. Consider a system having state model

$$\begin{bmatrix} \dot{X}_1 \\ \dot{X}_2 \end{bmatrix} = \begin{bmatrix} -2 & -3 \\ 4 & 2 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \end{bmatrix} + \begin{bmatrix} 3 \\ 5 \end{bmatrix} U \quad \text{and} \quad Y \begin{bmatrix} 1 & 1 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \end{bmatrix}$$

with $D = 0$ obtain its transfer function. (06 Marks)

OR

- 10 a. With a block diagram, explain sampled-data control system. (04 Marks)
- b. Consider a matrix 'A' given below:

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 3 & 0 & 2 \\ -12 & -7 & -6 \end{bmatrix}$$

Determine: (i) Eigen values (ii) Eigen vectors (iii) Modal matrix (06 Marks)

- c. Obtain the appropriate state model for a system represented by an electric circuit shown in Fig.Q10(c).

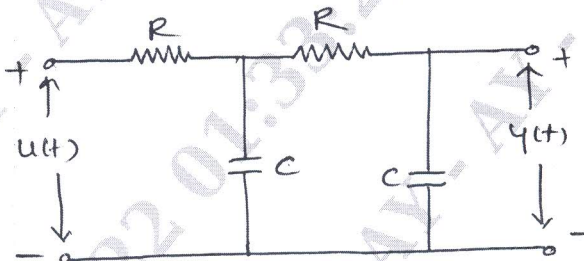


Fig.Q10(c)

(06 Marks)
