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15EE63

**Sixth Semester B.E. Degree Examination, Feb./Mar. 2022**  
**Digital Signal Processing**

Time: 3 hrs.

Max. Marks: 80

**Note: Answer any FIVE full questions, choosing ONE full question from each module.**

**Module-1**

- 1 a. Compute 4-point DFT of an input sequence :  $x(n) = \cos\left(\frac{n\pi}{4}\right)$  and plot its magnitude and phase angle. (06 Marks)
- b. Obtain the linear convolution of the sequences  $x(n) = \{1, 2, -1, 2, 3, -2, -3, -1, 1, 1, 2, -1\}$  and  $h(n) = \{1, 2\}$ , using overlap save method with 4 -point circular convolution. (10 Marks)

**OR**

- 2 a. Find the circular convolution of input sequence  $x(n) = \{1, 2, 3, 4\}$  with impulse response  $h(n) = \{2, 1, 2, 1\}$  using Stockham's method. (07 Marks)
- b. State and prove circular time shifting property of Discrete Fourier transform. (03 Marks)
- c.  $X(k)$  is a 14-point DFT of the sequence  $x(n)$ , the first 8-samples of  $X(k)$  are given as :  
 $X(0) = 12$ ;  $X(1) = (-1 + j3)$ ;  $X(2) = (3 + j4)$ ;  $X(3) = (1 - j5)$ ;  $X(4) = (-2 + j2)$ ;  $X(5) = (6 + j3)$   
 $X(6) = (2 - j3)$ ;  $X(7) = 10$ . Compute the remaining samples of  $X(k)$  and find the value of  
 $\sum_{n=0}^{13} |x(n)|^2$ . (06 Marks)

**Module-2**

- 3 a. Show that FFT is computationally efficient than direct computation of DFT. (04 Marks)
- b. What are the similarities and differences between DIT and DIF algorithms of FFT? (04 Marks)
- c. Compute 8-point DFT of the sequence  $x(n) = \{1, 1, 1, 1\}$  using Radix - 2 DIT - FFT algorithm. (08 Marks)

**OR**

- 4 a. If  $x_1(n) = \{1, 2, 0, 1\}$  and  $x_2(n) = \{1, 3, 3, 1\}$ , obtain the circular convolution of  $x_1(n)$  and  $x_2(n)$  using Radix - 2 DIT - FFT algorithm. (08 Marks)
- b. If DFT  $X(k)$  is given as :  
 $X(k) = \{0, 2\sqrt{2}(1-j), 0, 0, 0, 2\sqrt{2}(1+j)\}$ , determine the corresponding time sequence  $x(n)$  and draw the signal flow graph with all intermediate results, using inverse Radix - 2 DIF - FFT algorithm. (08 Marks)

**Module-3**

- 5 a. The system function of an analog filter is given as :  $H_a(s) = \frac{s+0.1}{(s+0.1)^2+9}$ . Obtain the system function of the IIR digital filter using impulse invariance method. (06 Marks)
- b. Design an analog filter with maximally flat response in the passband and an acceptable attenuation of -2dB at 20 radians/sec. The attenuation in the stopband should be more than 10dB beyond 30 radians/sec. (10 Marks)

OR

- 6 a. Design a lowpass 1rad/sec bandwidth Chebyshev filter with an acceptable passband ripple of 2dB, cut-off frequency of 1 rad/sec and stopband attenuation of 20dB or greater beyond 1.3 rad/sec. (10 Marks)
- b. Use Bilinear transformation to design a first order lowpass Butterworth filter that has a 3dB cut-off frequency at  $W_c = 0.2\pi$ . The normalized filter is given as :
- $$H_{an}(s) = \frac{1}{s+1}. \quad (06 \text{ Marks})$$

Module-4

- 7 a. Design a digital lowpass filter using Chebyshev filter design procedure that meets the following specifications : passband magnitude characteristics that is constant to 1dB for frequencies below  $w = 0.2\pi$  and stopband attenuation of at least 15dB for frequencies between  $w = 0.3\pi$  and  $\pi$ . Use Bilinear transformation. (10 Marks)
- b. Obtain the general realization of parallel form for an IIR system. (06 Marks)

OR

- 8 a. Design a Chebyshev filter for the following specifications using impulse invariance method.  
 $0.8 \leq |H(e^{j\omega})| \leq 1$  for  $0 \leq \omega \leq 0.2\pi$  (12 Marks)  
 $|H(e^{j\omega})| \leq 0.2$  for  $0.6\pi \leq \omega \leq \pi$
- b. A difference equation describing a filter is given as :
- $$y(n) - \frac{3}{4}y(n-1) + \frac{1}{8}y(n-2) = x(n) - \frac{1}{2}x(n-1)$$
- Draw Direct form – I and Direct form – II structures for an IIR system. (04 Marks)

Module-5

- 9 a. Design a normalized linear phase FIR filter having the phase delay of  $\tau = 4$  and atleast 40dB attenuation in the stopband. Also obtain the magnitude/frequency response of the filter. (12 Marks)
- b. Obtain the cascade realization of the system function :
- $$H(z) = 1 + \frac{5}{2}z^{-1} + 2z^{-2} + 2z^{-3}. \quad (04 \text{ Marks})$$

OR

- 10 a. Design a low pass FIR filter using frequency sampling technique having cut-off frequency of  $\frac{\pi}{2}$  rad/sample. The filter should have a linear phase with length  $M = 17$ . (12 Marks)
- b. Determine the direct form realization of the system function :
- $$H(z) = 1 + 2z^{-1} - 3z^{-2} - 4z^{-3} + 5z^{-4}. \quad (04 \text{ Marks})$$

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