

20MMD11

First Semester M.Tech. Degree Examination, Jan./Feb. 2021 Mathematical Methods in Engineering

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

- Define: i) Error ii) Roundoff Error iii) Relative Error iv) Truncation Error and find the value of $s = \frac{x^2 \sqrt{y}}{z^3}$ where $x = 6.54 \pm 0.01$, $y = 48.64 \pm 0.02$ and $z = 13.5 \pm 0.03$. Also find the relative error in the result.
 - A horizontal tie-rod is freely pinned at each end. It carries a uniform load 'w' lb per unit length and has a horizontal pull 'P'. Find the central deflection and the maximum bending moment, taking origin at one of its ends. (10 Marks)

- OR The differential equation for the displacement 'y' of a whirling shaft when weight of the shaft is taken into account is $EI\frac{d^4y}{dx^4} - \frac{Ww^2}{g}y = W$. Taking the shaft of length '21' with the origin at the centre and short bearings at both ends, show that the maximum deflection of the shaft is $\frac{g}{2w^2}$ (sechal + secal-2) (10 Marks)
 - b. Derive the expression $v(t) = \frac{gm}{c}(1 e^{-\frac{c}{m}t})$ for a parachutist jumps out of a stationary hot air balloon. Compute the velocity attained after 10 seconds. Mass of parachutist is 68.1kg. The drag coefficient is equal to 12.5 kg/s. Gravitational force is 9.8m/s^2 (Take t=2 sec as step size). (10 Marks)

Module-2

a. Solve the system of equations by using Gauss Jordan method

$$\begin{bmatrix} 1 & -1 & 2 \\ 1 & 1 & 1 \\ 2 & -2 & 3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -8 \\ -2 \\ -20 \end{bmatrix}$$

(10 Marks)

Use Givens technique on the tridiagonal matrix generated in

$$\mathbf{A} = \begin{bmatrix} 4 & -2 & 1 & 2 \\ -2 & 3 & 0 & -2 \\ 1 & 0 & 2 & 1 \\ 2 & -2 & 1 & -1 \end{bmatrix}$$

To obtain the ranges of integers between which the four roots of the characteristic equation (10 Marks)

4 a. Solve by Cholesky's method

 $4x_1 - x_2 = 1$; $-x_1 + 4x_2 - x_3 = 0$; $-x_2 + 4x_3 - x_4 = 0$; $-x_3 + 4x_4 = 0$. (10 Marks)

b. Find the inverse of the matrix by Partition method.

 $\begin{bmatrix} 2 & 1 & 0 & 0 \\ 1 & 2 & 1 & 0 \\ 0 & 1 & 2 & 1 \\ 0 & 0 & 1 & 2 \end{bmatrix}$ (10 Marks)

Module-3

- 5 a. Solve $\frac{dy}{dx} = 1 + xy$, y(0) = 1. Find y(0.1) using Picards method upto fourth approximation.
 - b. Given $\frac{dy}{dx} = z y$, $\frac{dz}{dx} = y z$ with y(0) = 1 and z(0) = 0. Solve by Runge-Kutta method of second order choosing h = 0.05. Obtain the value of 'y' at x = 0.1. (10 Marks)

OR

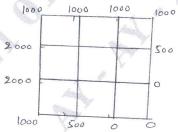
- 6 a. Find the real roots of the equation $x^3 6x^2 + 11x 6 = 0$ by Graffe's method. (10 Marks)
 - b. Find the root of the equation $y(x) = x^3 2x 5 = 0$ which lie between 2 and 3 by Muller's method. (10 Marks)

Module-4

7 a. Solve $\frac{\partial^2 u}{\partial t^2} = 4 \frac{\partial^2 u}{\partial x^2}$ explicitly with the initial and the boundary conditions

 $u(x, 0) = x^2(1 - x^2)$, $\frac{\partial u}{\partial t}(x, 0) = 0$, u(0, t) = 0, u(1, t) = 0 with $\Delta x = \frac{1}{4}$, $\Delta t = \frac{1}{64}$. Obtain the solution at first time level.

b. Given the values of $\phi(x, y)$ on the boundary of the square in the below. Evaluate the function $\phi(x, y)$ satisfying the Laplace equation $\nabla^2 \phi = 0$ at the pivoted points by Gauss Siedel method. (10 Marks)



OR

- 8 a. Solve $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$, $t \ge 0$, $0 \le x \le 1$, u(x, 0) = x(1 x), $\begin{cases} u(0, t) = 0 \\ u(1, t) = 1 \end{cases}$ $t \ge 0$ $\Delta x = \frac{1}{4}$, $\Delta t = \frac{1}{64}$, Using Schmidt method at second time level.
 - b. Consider the equation $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ where $0 \le x$, $y \le 1$ subjected to u(x, 0) = x, u(x, 1) = 0, $0 \le x \le 1$, u(0, y) = 0, u(1, y) = 0, $0 \le y \le 1$. Choose $\Delta x = \Delta y = h = \frac{1}{3}$. Solve the system of linear equations by four iterations of Gauss Seidel method. (10 Marks)

Module-5

A set of five similar coins tossed 320 times and the result is

Number of heads: 0 1 2 3

Frequency: 6 27 72 112 71

Test the hypothesis that the data follow a binomial distribution.

(10 Marks)

b. Explain and illustrate the Random Block Design (RBD).

(10 Marks)

OR

Measurements on the length of a copper wire were taken in 2 experiments A and B as under. 10 a.

A's measurement 12.29 12.25 11.86 12.13 B's measurement 12.39 12.46 12.34 12.22

A's measurement 12.78 12.77 11.90 12.47

12.46 12.23 B's measurement 12.06

(10 Marks)

b. Suppose a person claims that Lorry Bird's free throw success follow a binomial distribution with P = 0.80. For the 1980-81 and 1981-82 seasons Lorry Bird shot 338 pairs of free throws with the following results:

Number of Makes: 0

Observed count: 5 82 251

Calculate the pair of free throws using chi square distribution.

(10 Marks)