

18MT34

## Third Semester B.E. Degree Examination, July/August 2021 Control Systems

Time: 3 hrs.

4L ORE

Max. Marks: 100

Note: Answer any FIVE full questions.

a. Compare open loop and closed loop control system.

(10 Marks)

b. For the Fig Q1(b) shown below, determine TF  $\frac{x_2(s)}{x_1(s)}$ 

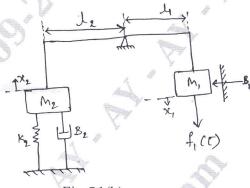


Fig Q1(b)

(10 Marks)

a. Draw the analogous circuits using F-V and F-I analogy for the mechanical system shown below Fig Q2(a)

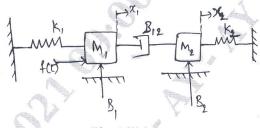


Fig Q2(a)

(12 Marks)

b. Obtain  $\frac{C(s)}{R(s)}$  using Block diagram reduction rules for the Fig Q2(b) shown below :

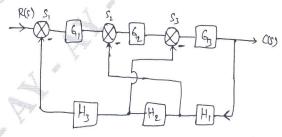


Fig Q2(b)

(08 Marks)

3 a. Construct the SFG for the set of system equations :  $y_2 = G_1y_1 + G_3y_3$ ;  $y_3 = G_4y_1 + G_2y_2 + G_5y_3$ ;  $y_4 = G_6y_2G_7y_3$  where  $y_4$ is output

Find transfer function.

y 4 y 1

Using Maron's Gain formula

(10 Marks)

b. For the SFG shown in Fig Q3(b) below, find  $\frac{C(s)}{R(s)}$  by Maron's Gain Formula.

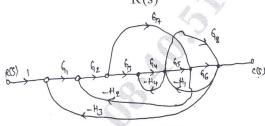


Fig Q3(b)

(10 Marks)

- 4 a. With a neat output versus time graph define the following i) Delay Time (t<sub>d</sub>) ii) Rise time (t<sub>r</sub>) iii) Peak time (t<sub>p</sub>) iv) Maximum overshoot (M<sub>P</sub>) (10 Marks)
  - b. For a system having  $G(s) = \frac{15}{(s+1)(s+3)}$ , H(s) = 1. Determine:
    - i) Characteristics equation ii) w<sub>n</sub> and ξ [natural frequency and damping factor]
    - iii) Time at which first undershoot will occur iv) Time period of oscillations related to w<sub>d</sub>
    - v) Number of cycles output will perform before setting down for ±2% tolerance.

(10 Marks)

- 5 a. Define the following: i) Absolute stability ii) Relative stability iii) Conditionally stable iv) Marginally stable. (04 Marks)
  - b. For unity feedback system  $G(s) = \frac{k}{s(1+0.4s)(1+0.25s)}$  find the range of values of k,
  - marginar value  $\kappa$  and frequency of oscillation (w). c. For a system with C.E – characteristics equation F(s) =  $s^6 + 3s^5 + 4s^4 + 6s^3 + 5s^2 + 3s + 2 = 0$ . Examine stability. (08 Marks)
- 6 a. State the advantages and limitation of frequency domain approach. (08 Marks)
  - b. Explicitly discuss the correlation between time and frequency response of a second order system. Obtain the expression for resonant peak. (12 Marks)
- Draw the appropriate root locus diagram for the closed loop system whose transfer function is given by G(s).  $(H(s) = \frac{k}{s(s+2)(s^2+6s+25)}$  comment on stability. (20 Marks)
- Sketch Bode plot for the transfer function  $G(s) = \frac{k.s^2}{(1+0.25)(1+0.025)}$ . Determine valve of 'k' for gain cross over frequency to be 5 rads<sup>-1</sup>. (20 Marks)
- 9 a. Define: i) State variable ii) State vector iii) State space iv) State trajectory. (08 Marks) b. List the advantages of state variable analysis. (05 Marks)
  - c. Obtain the transfer function: If  $\begin{bmatrix} \dot{\mathbf{x}}_1 \\ \dot{\mathbf{x}}_2 \end{bmatrix} = \begin{bmatrix} -5 & -1 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{x}_2 \end{bmatrix} + \begin{bmatrix} 2 \\ 5 \end{bmatrix} \mathbf{u} \quad \mathbf{y} = \begin{bmatrix} 12 \end{bmatrix} \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{x}_2 \end{bmatrix}$  (07 Marks)
- a. Lit the properties of state transition matrix and write the equation for transfer function from state model. (10 Marks)
  - b. Consider a control system with state model

 $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 2 \end{bmatrix} u ; \begin{bmatrix} x_1(0) \\ x_2(0) \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} u = \text{unit step.} \quad \text{Compute the state transfer matrix and there from find the state response i.e., } x(t)$ (10 Marks)