15EC36

Third Semester B.E. Degree Examination, July/August 2021 Engineering Electromagnetics

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions.

- a. State and explain Coulomb's law of force between two point charges and mention the units of quantities in the force equation. (06 Marks)
 - b. Three equal charges of 1 μC each are located at the three corners of a square of 10 cm side.
 Find the electric field intensity at the forth vaccent point of the square.
- 2 a. A line charge $\rho_L = 50$ nC/m is located along the line x = 2, y = 5 in free space. Find $\stackrel{\rightarrow}{E}$ at P(1, 3, -4).
 - b. Derive the expression of electric field intensity due to infinite line charge.

(10 Marks)

3 a. State and prove the Gauss's law.

- (10 Marks)
- b. Given the flux density $\vec{D} = \frac{5\sin\theta.\cos\phi}{r} \hat{a}_r$ C/m². Find (i) Volume charge density
 - (ii) Total flux leaving the surface of spherical volume of radius 2 m.
- (06 Marks)

4 a. State and derive the expression of law of continuity of current.

(07 Marks)

b. An electric potential is given by,

$$V = \frac{60 \sin \theta}{r^2}$$
 volt. Find V and E at point P(3, 60°, 25°).

(06 Marks)

c. Express $\overrightarrow{\nabla}.\overrightarrow{D}$ in three coordinate systems.

- (03 Marks)
- 5 a. Starting from Gauss's law in integral form, derive Laplace's and Poisson's equations. Write the Laplace equation in all the coordinate systems. (06 Marks)
 - b. Determine whether or not the following vectors represent a possible electric field:

$$\vec{E} = (12yx^2 - 6z^2x)\hat{a}_x + (4x^3 + 18zy^2)\hat{a}_y + (6y^3 - 6zx^2)\hat{a}_z$$

(03 Marks)

c. State and prove uniqueness theorem.

- (07 Marks)
- 6 a. State Biot-Savart law. Obtain an expression for magnetic field intensity for current element.
 (08 Marks)
 - b. Explain the concept of scalar and vector magnetic potential and show that

$$\vec{A} = \frac{\mu_0}{4\pi} \int \frac{\vec{J}}{r} dV$$
. where \vec{A} = Vector magnetic potential and J = current density (08 Marks)

- 7 a. Write short notes on force between two differential current elements. (08 Marks)
 - b. A point charge $\theta = -60 \, \text{nC}$, is moving with a velocity $6 \times 10^6 \, \text{m/s}$ in the direction specified by unit vector $(-0.48 \hat{a}_x 0.6 \hat{a}_y + 0.64 \hat{a}_z)$. Find the magnitude of the force on a moving charge in the magnetic field

$$\vec{B} = (2\hat{a}_x - 6\hat{a}_y + 5\hat{a}_z) \text{mT}.$$
 (08 Marks)

- 8 a. Derive the expression for the boundary condition for the tangential component at the interface between two media with different permeabilities. (06 Marks)
 - b. If $\vec{B} = 0.5x\hat{a}_yT$ in a material for which $\chi_m = 2.5$ find,

(i) μ_r (ii) μ (iii) \vec{H} (iv) \vec{M} (v) \vec{J} . (10 Marks)

9 a. Write Maxwell equations in points form and integral form. (06 Marks)

b. State and prove Faraday's law. (05 Marks)

c. Given $\overrightarrow{H} = H_m e^{j(\omega t + \beta z)} \hat{a}_x$ A/m in free space. Find \overrightarrow{E} . (05 Marks)

10 a. Derive the expression for Poynting's theorem. (10 Marks)

b. Write the short notes on skin effect. (06 Marks)