Time 13



Second Semester B.E. Degree Examination, Jan./Feb.2021

Engineering Mathematics – II

15MAT21

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

a. Solve by inverse differential operator method,

$$\frac{d^3y}{dx^3} - 4\frac{dy}{dx} = 3e^{2x} + 10.$$
 (05 Marks)

b. Solve by Inverse differential operator method,

$$\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = xe^x \sin x. \tag{05 Marks}$$

c. Solve by variation of parameters method
$$\frac{d^2y}{dx^2} + y = \tan x$$
. (06 Marks)

OR

2 a. Solve
$$(D^3 + 1)y = \cos x$$
. (05 Marks)

b. Solve
$$(D^2 - 2D)y = x^2 + 2x + 1$$
. (05 Marks)

c. Solve by undetermined coefficients method
$$(D^2 + 3D + 2)y = 2e^{-x} + x^2$$
. (06 Marks)

Module-2

3 a. Solve
$$x^2 \frac{d^2y}{dx^2} - x \frac{dy}{dx} + y = \log x$$
. (05 Marks)

b. Solve
$$xy\left(\frac{dy}{dx}\right)^2 - (x^2 + y^2)\frac{dy}{dx} + xy = 0$$
. (05 Marks)

c. Solve
$$y = 2px + tan^{-1}(xp^2)$$
. (06 Marks)

OR

4 a. Find the general and singular solution of the equation, $\sin px \cos y = \cos px \sin y + p$. (05 Marks)

b. Solve
$$p = \tan \left[x - \frac{p}{1 + p^2} \right]$$
. (05 Marks)

c. Solve the Legendre's linear equation,

$$(1+x)^2y'' + (1+x)y' + y = 2\sin[\log(1+x)].$$
 (06 Marks)

Module-3

5 a. Form the partial differential equation by eliminating the orbitrary functions from, z = f(y + 2x) + g(y - 3x). (05 Marks)

b. Solve the partial differential equation,

$$\frac{\partial^3 z}{\partial x^2 \partial y} = \cos(2x + 3y), \text{ by direct integration.}$$
 (05 Marks)

c. With usual notations derive the one dimensional wave equation as, $\frac{\partial^2 u}{\partial t^2} = C^2 \frac{\partial^2 u}{\partial x^2}$. (06 Marks)

(05 Marks) a. Form the partial differential equation from $z = (x + y)f(x^2 - y^2)$.

b. Solve
$$\frac{\partial^2 z}{\partial x^2} + 5\frac{\partial z}{\partial x} + 6z = 0$$
 with $z = 0$ and $\frac{\partial z}{\partial x} = e^{-y}$ at $x = 0$. (05 Marks)

Solve one dimensional heat equation by variable seperable method as, $\frac{\partial y}{\partial t} = C^2 \frac{\partial^2 y}{\partial x^2}$. (06 Marks)

Change the order of integration and hence evaluate,

$$\int_{0}^{a} \int_{y}^{a} \frac{x}{x^2 + y^2} dxdy. \tag{05 Marks}$$

b. Evaluate
$$\int_{0}^{1} \int_{y^2}^{1} \int_{0}^{1-x} x \, dz dx dy.$$
 (05 Marks)

c. Prove that
$$\beta(m,n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$$
. (06 Marks)

a. Evaluate by Changinginto polar co-ordinates.

$$\int_{0}^{1} \int_{0}^{\sqrt{1-y^2}} (x^2 + y^2) dx dy.$$
 (05 Marks)

b. Find the volume of the sphere, $x^2 + y^2 + z^2 = a^2$ by triple integration. (05 Marks)

c. Prove that $\int_0^1 \frac{x^2}{\sqrt{1-x^4}} dx \times \int_0^1 \frac{dx}{\sqrt{1+x^4}} = \frac{\pi}{4\sqrt{2}}$ by using Beta gamma functions. ; (06 Marks)

Find the Laplace transform of $(1 + te^{-t})^3$.

(05 Marks)

- Find the Laplace transform of the function, $f(t) = E \sin \omega t$, $0 < t < \frac{\pi}{\omega}$, having the period $\frac{\pi}{\omega}$.
- c. Using Laplace transform techniques, solve $\frac{d^2x}{dt^2} 2\frac{dx}{dt} + x = e^t$ with x = 2, $\frac{dx}{dt} = -1$ at t = 0. (06 Marks)

a. Find the Laplace transforms of,

(i)
$$t \cos t$$
 and (ii) $\frac{\sin^2 t}{t}$. (05 Marks)

b. Find
$$L^{-1} \left[\log \sqrt{\left(\frac{s^2 + b^2}{s^2 + a^2} \right)} \right]$$
 (05 Marks)

c. Use convolution theorem to evaluate
$$L^{-1}\left[\frac{1}{(s+a)(s+b)}\right]$$
. (06 Marks)