

15EC52

Fifth Semester B.E. Degree Examination, Aug./Sept. 2020 Digital Signal Processing

Time: 3 hrs.

Max. Marks: 80

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.
2. Use of Normalized filters tables is permitted.

Module-1

- a. Compute the circular convolution of the following sequences using DFT and 1DFT method $x(n) = \{1, 2, 3, 4\}$ and $h(n) = \{4, 3, 2, 1\}$. (08 Marks)
 - b. Given $x(n) = \{1, -2, -2, 5, 8, 2\}$, evaluate the given expression $\sum_{K=0}^{5} e^{-j2\pi k/3} x(K)$ without computing DFT. (04 Marks)
 - c. Obtain the relationship of DFT with z-transforms.

(04 Marks)

OR

- a. Explain frequency domain sampling and reconstruction of signals.
- (09 Marks)

- Consider the finite length sequence $x(n) = \delta(x) + 2\delta(n-5)$ i) Find the 10 point DFT of x(n)
- ii) Find the sequence that has a DFT $y(k) = e^{\frac{j2k2\pi}{10}}x(k)$

(07 Marks)

Module-2

- 3 a. Evaluate the linear convolution of the following sequences using DFT and 1DFT method. $x(n)=\{1,2,3\}$ and $h(n)=\{1,2,2,1\}$. (08 Marks)
 - b. A long sequence x(n) is filtered through a filter with impulse response h(n) to yield the output y(n). If $x(n) = \{1, 1, 1, 1, 1, 3, 1, 1, 4, 2, 1, 1, 3, 1\}$ and $h(n) = \{1, -1\}$. Compute y(n) using overlap save technique. Use only a 5-point circular convolution. (08 Marks)

OR

- 4 a. State and prove the following properties of DFT i) Parseval's theorem
 ii) Time shifting property. (04 Marks)
 - b. Determine the response of an LTI system with $h(n) = \{1, -1, 2\}$ for an input $x(n) = \{1, 0, 1, -2, 1, 2, 3, -1, 0, 2\}$ use overlap add method with block length L = 4.

(06 Marks)

Module-3

- 5 a. Find the DFT of the sequence using decimation in time FFT algorithm and draw the flow graph indicating the intermediate values in the flow graph. $x(n) = \{1, -1, -1, 1, 1, 1, -1\}.$ (08 Marks)
 - b. Derive the computational arrangement of 8-point DFT using radix 2 DIF-FFT algorithm.
 (08 Marks)

OR

- 6 a. What is Goertzel algorithm? Obtain direct form-II realization of second order goertzel filter.
 (08 Marks)
 - b. Find the 1DFT of the sequence using DIF-FFT algorithm: $X(k) = \{0, 2\sqrt{2}(1-j), 0, 0, 0, 0, 2\sqrt{2}(1+j).$ (08 Marks)

Module-4

Draw the block diagrams of direct form – I and direct form – II realizations for a digital IIR filter described by the system function:

 $H(z) = \frac{8z^3 - 4z^2 + 11z - 2}{(z - \frac{1}{4})(z^2 - z + \frac{1}{2})}.$ (08 Marks)

b. Show that the bilinear transformation maps the s-plane to z-plane efficiently in the (08 Marks) transformation of analog to digital filter.

OR

Design a two pass Butterworth analog filter to meet the following specifications:

i) Attenuation of -1 db at 20rad/sec

ii) Attenuation is greater than 20db beyond 40rad/sec.

b. The transfer function of analog filter is $H(s) = \frac{2}{(s+1)(s+2)}$. Find H(z) using impulse (07 Marks) invariance method. Show H(z) when $T_S = 1$ sec.

Module-5

A low pass filter is to be designed with the following desired frequency response

A low pass litter is to be designed with the following H_d(e^{j\omega}) = H_d(\omega) =
$$\begin{cases} e^{-j2\omega}; & |\omega| < \frac{\pi}{4} \\ 0; & \frac{\pi}{4} < |\omega| < \pi \end{cases}$$

Determine the filter coefficients $h_d(n)$ and h(n) if $\omega(n)$ is a rectangular window defined as

follows:
$$\omega_{R}(n) = \begin{cases} 1; & 0 \le n \le 4 \\ 0; & \text{otherwise} \end{cases}$$

(08 Marks)

$$h(n) = \delta(n) + \frac{1}{4}\delta(n-1) - \frac{1}{8}\delta(n-2) + \frac{1}{4}\delta(n-3) + \delta(n-4).$$
(08 Marks)

The frequency response of an FIR filter is given by:

 $H(\omega) = e^{-j3\omega} (1 + 1.8\cos 3\omega + 1.2\cos 2\omega + 0.5\cos \omega).$

Determine the coefficients of the impulse response h(n) of the FIR filter.

(06 Marks)

- b. Obtain the coefficients of FIR filter to meet the specification given below using the window
 - i) Pass band edge frequency $f_p = 1.5 \text{KHz}$

ii) Stop band edge frequency $f_s = 2KHz$

iii) Minimum stop band attenuation = 50db (Hamming)

iv) Sampling frequency F_s = 8KHz.

(10 Marks)