

BANGA

Sixth Semester B.E. Degree Examination, Aug./Sept.2020 Theory of Elasticity

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, selecting atleast TWO questions from each part.

PART - A

- 1 a. Explain: i) Stress at a point ii) Strain at a point. (10 Marks)
 - b. Explain the assumptions made in theory of elasticity, and also its applications. (10 Marks)
- 2 a. Derive the differential equations of equilibrium in two dimensional Cartesian co-ordinates.
 (10 Marks)
 - b. What is an Airy's stress function? Explain its importance in the theory of elasticity.

(10 Marks)

- 3 a. Define the following with sketches and suitable examples:
 - i) Plane stress problems ii) Plane strain problems. (10 Marks)
 - b. By means of a strain rosette, the following strains, were recorded during the test on a structural member. $\epsilon_{\phi} = 2 \times 10^{-3}$, $\epsilon_{(\alpha+\phi)} = 1.35 \times 10^{-3}$, $\epsilon_{(\alpha+\beta+\phi)} = 0.95 \times 10^{-3}$.

Determine i) Magnitude of principal strains and ii) Orientation of principal planes. Given that: $\phi = 0^{\circ}$, $\alpha = \beta = 45^{\circ}$, $\mu = 0.33$, E = 210 GPa. (10 Marks)

Find the expressions of stress for a bending of simply supported beam subjected to uniformly distributed loading. (20 Marks)

PART - B

- 5 a. Derive the partial differential equations of equilibrium in polar coordinates for 2 dimensional system. (10 Marks)
 - b. Check if $\phi = -\frac{P}{\pi}r \theta \sin \theta$ represents a stress function. (10 Marks)
- 6 a. Define Axi-symmetric problem with example. (06 Marks)
 - b. Derive Lame's equation for thick cylinders. (14 Marks)
- 7 Discuss the effect of circular hole on stress distribution in plate subjected to uniform tensile stress 'P'. (20 Marks)
- 8 a. Derive the differential equation of torsion in the form $\nabla^2 \phi = -2G\theta$. (10 Marks)
 - b. Prove that the angle of twist of an elliptical section with major axis '2a' and minor axis '2b'

is given by
$$\theta = \frac{T(a^2 + b^2)}{\pi a^3 b^3 G}$$
. (10 Marks)