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15AU73

Seventh Semester B.E. Degree Examination, Aug./Sept.2020

## Finite Element Modeling and Analysis

Time: 3 hrs.

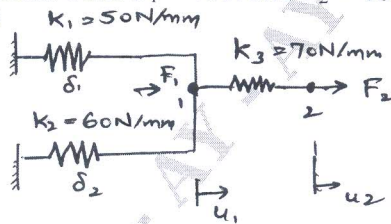
Max. Marks: 80

*Note: Answer any FIVE full questions, choosing ONE full question from each module.*

### Module-1

- 1 a. Explain with neat sketch plane stress and plane strain. (08 Marks)
- b. For the spring system shown in Fig.Q.1(b) using principle of minimum potential energy determine the nodal displacement. Take  $F_1 = 75\text{N}$  and  $F_2 = 100\text{N}$ . (08 Marks)

Fig.Q.1(b)



OR

- 2 a. Derive the equilibrium equation for 3D elastic body. (08 Marks)
- b. By RR method for a bar of cross section area A, elastic modulus E, subjected to uniaxial loading P. Show that a distance X from fixed end is  $u = \left(\frac{P}{AE}\right)X$  (08 Marks)

### Module-2

- 3 a. What is FEA? Explain the basic steps involved in FEM. (08 Marks)
- b. Derive the stiffness matrix for the bar subjected to axial load F using direct method. (08 Marks)

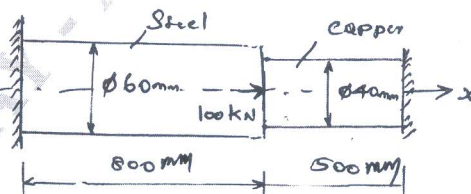
OR

- 4 a. What is shape function? Derive the shape function for 1D bar element in global coordinates. (08 Marks)
- b. What are the convergence requirements? Discuss three condition of convergence requirement. (08 Marks)

### Module-3

- 5 a. Determine the nodal displacement stress in each element and support reaction in the bar shown in Fig.Q5(a). (08 Marks)

Fig.Q5(a)



- b. Solve the following system of simultaneous equation by gauss elimination method:

$$4x_1 + 2x_2 + 3x_3 = 4$$

$$2x_1 + 3x_2 - 5x_3 = 2$$

$$2x_1 + 7x_2 = 4$$

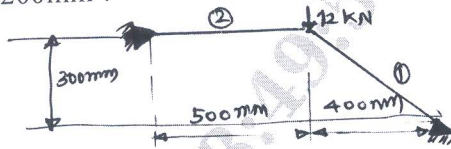
(08 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 = 50, will be treated as malpractice.

OR

- 6 a. For the two bar truss shown in Fig.Q.6(a). Determine the nodal displacements. (08 Marks)  
 Take  $E = 2 \times 10^5 \text{MPa}$ ,  $A = 200 \text{mm}^2$ .

Fig.Q.6(a)



- b. Derive the elemental stiffness matrix for a truss element. (08 Marks)

**Module-4**

- 7 a. Derive the shape function using lagrangian interpolation for linear Quadrilateral element. (08 Marks)  
 b. Briefly explain subparametric elements and super parametric elements. (08 Marks)

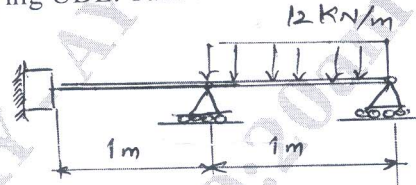
OR

- 8 a. Derive the hermite shape function for a 2 noded beam element. (08 Marks)  
 b. Briefly explain the finite element formulation of 2D Constant Strain Triangular Element (CST). (08 Marks)

**Module-5**

- 9 a. For the beam shown in Fig.Q.9(a). Determine the end reaction and deflection at the center of the portion of the beam carrying UDL. Take  $E = 200 \text{GPa}$   $I = 4 \times 10^6 \text{mm}^4$ . (08 Marks)

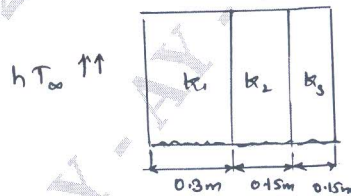
Fig.Q.9(a)



- b. Solve for temperature distribution in the composite wall as shown in Fig.Q.9(b) using 1D heat elements, use penalty approach of handling boundary conditions.

$K_1 = 20 \text{W/m}^\circ\text{C}$   
 $K_2 = 30 \text{W/m}^\circ\text{C}$   
 $T_0 = 20^\circ\text{C}$   
 $K_3 = 50 \text{W/m}^\circ\text{C}$   
 $h = 25 \text{W/m}^2\text{C}$

Fig.Q.9(b)

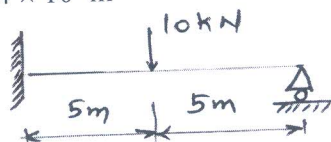


(08 Marks)

OR

- 10 a. Derive the expression for stiffness matrix for 1D heat conduction. (08 Marks)  
 b. For the beam element shown in Fig.Q.10(b). Determine deflection under the given load. (08 Marks)  
 Take  $E = 2 \times 10^8 \text{kN/m}^2$  and  $I = 4 \times 10^{-6} \text{m}^4$

Fig.Q.10(b)



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