

CBCS SCHEME

USN



15AE651

Sixth Semester B.E. Degree Examination, Aug./Sept. 2020

Finite Element Method

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Explain plane stress and plane strain problems in FEM. (08 Marks)
 b. For the spring system shown in Fig.Q1(b). Determine the nodal displacements. Take $F_1 = 75\text{N}$, $F_2 = 100\text{N}$.

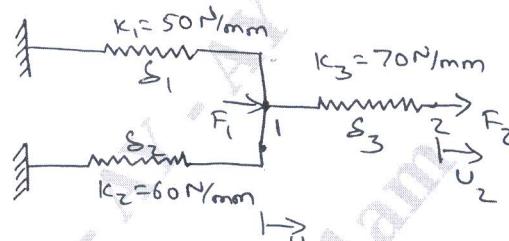


Fig.Q1(b)

(08 Marks)

OR

- 2 Using Rayleigh – Ritz, find the displacement at midpoint of a beam as shown in Fig.Q2 carries a central point load 'P' having Young's modulus 'E' and cross sectional area 'A'.

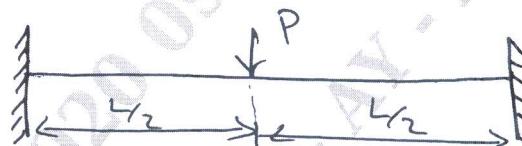


Fig.Q2

(16 Marks)

Module-2

- 3 a. Determine the nodal displacement, stress in each element and support reaction in the bar shown in Fig.Q3(a) due to applied load $P = 100\text{kN}$ take $E_{\text{steel}} = 200 \text{ GPa}$; $E_{\text{cu}} = 100 \text{ GPa}$.

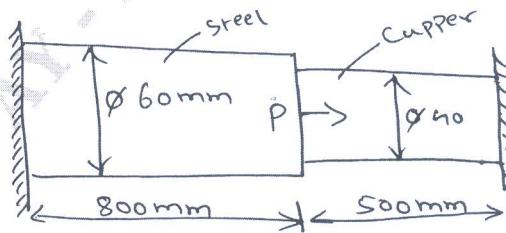


Fig.Q3(a)

(08 Marks)

- b. Write Hermite function for beam element with usual notations. (08 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
 2. Any revealing of identification, appeal to evaluator and / or equations written eg, $42+8=50$, will be treated as malpractice.

OR

- 4 For 2 bar truss shown in Fig.Q4 determine the nodal displacements and the stress in each member. Take $E = 200 \text{ GPa}$.

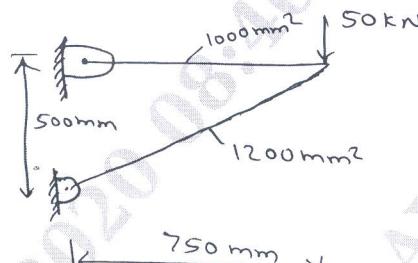


Fig.Q4

(16 Marks)

Module-3

- 5 a. Derive shape function for quadrilateral element in natural co-ordinate system considering nine nodes. (08 Marks)
 b. The nodal co-ordinates of a triangular element are shown in Fig.Q5(b). The X-coordinate of point P is 3.3 and shape function $N_1 = 0.3$. Determine N_2 , N_3 and Y – coordinate of point P.

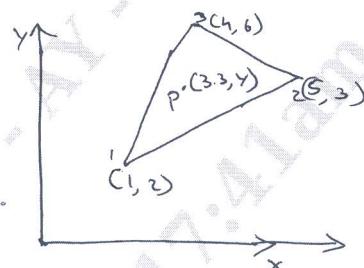


Fig.Q5(b)

(08 Marks)

OR

- 6 a. Derive shape function of simple tetrahedral element in natural co-ordinate system. (08 Marks)
 b. Determine the Jacobian of the transformations J for triangular element shown in Fig.Q6(b). Also find the area of triangle.

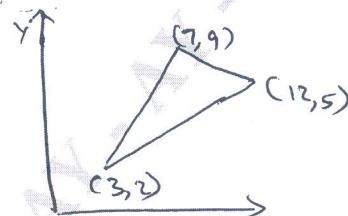


Fig.Q6(b)

(08 Marks)

Module-4

- 7 a. Explain isoparametric, subparametric and superparametric elements. (08 Marks)
 b. Using Gaussian 2 point formula evaluate following :

$$\text{i) } I = \int_{-1}^1 (1 + r + 2r^2 + 3r^3) dr$$

$$\text{ii) } I = \int_{-1}^1 (3e^\xi + \xi^2 + \frac{1}{\xi+2}) d\xi$$

(08 Marks)

OR

- 8 a. Explain computer program for structure for FEM analysis. (08 Marks)
 b. Explain formulation of global co-ordinate system of axisymmetric triangular element to local co-ordinate system. (08 Marks)

Module-5

- 9 Solve for temperature distribution in the composite wall as shown in Fig.Q9, using 1 – D elements.

$$K_1 = 20 \text{ w/m}^{\circ}\text{C}$$

$$K_2 = 30 \text{ w/m}^{\circ}\text{C}$$

$$K_3 = 50 \text{ w/m}^{\circ}\text{C}$$

$$T_{\infty} = 800^{\circ}\text{C}$$

$$h = 25 \text{ w/m}^2{}^{\circ}\text{C}$$

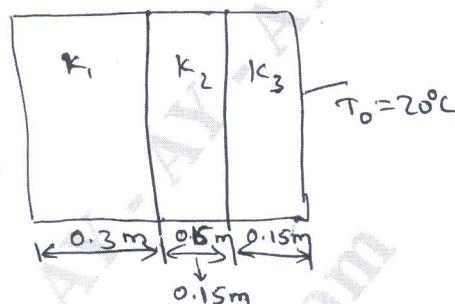


Fig.Q9

(16 Marks)

OR

- 10 Find the natural frequencies of longitudinal vibration of constrained stepped bar shown in Fig.Q10.

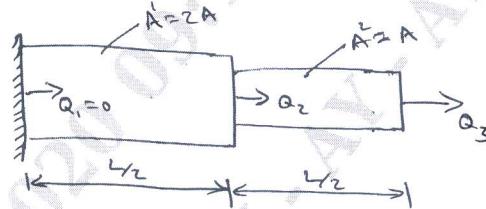


Fig.Q10

(16 Marks)
