USN

15EE54

Fifth Semester B.E. Degree Examination, Dec.2019/Jan.2020 Signals & Systems

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

Categorize the following signal as energy signal or power signal. Find out corresponding

$$x(t) = \begin{cases} t & 0 \le t \le 1\\ 2 - t & 1 \le t \le 2\\ 0 & \text{Otherwise} \end{cases}$$

(04 Marks)

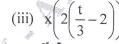
What are different elementary signals? Explain them with neat sketch.

(04 Marks)

Sketch and label for each of the following for given signal x(t) shown in Fig. Q1 (c):

(i)
$$x(2t+1)$$

(ii) x(-2t+3)



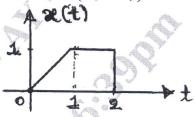


Fig. Q1 (c)

(08 Marks)

Explain different classification of signals. 2

(05 Marks)

- Given discrete time system $y(n) = 2x(2^n)$. Determine whether the system is,
 - (i) Linear
- (ii) Time variant
- (iii) Memoryless

(iv) Stable.

(05 Marks)

c. Find the even and odd part of the following signal,

(i)
$$x(t) = e^{-2t} \cos(t)$$

(ii)
$$x(t) = e^{jt}$$

(06 Marks)

Module-2

Find the following convolution sum $y(n) = \left(\frac{3}{4}\right)^n u(n) * u(n-2)$ and evaluate the value for 3 $n = \pm 5$.

(06 Marks)

Find out the total response of the system given by,

$$\frac{d^{2}}{dt^{2}}y(t) + 3\frac{d}{dt}y(t) + 2y(t) = 2x(t)$$

with
$$y(0) = -1$$
, $\frac{dy(t)}{dt}\Big|_{t=0} = 1$ and $x(t) = \cos(t)u(t)$

(10 Marks)

OR

- The impulse response of an LTI system is given by h(t) = u(t) u(t-2). Find the output of the system for a given input x(t) = u(t) - u(t-3). Draw the output response.
 - Draw the direct form I and direct form II implementations for the following difference

$$y[n] + \frac{1}{2}y[n-1] - y[n-3] = 3x[n-1] + 2x[n-2]$$
(06 Marks)

Find the Fourier Transform (FT) of the following signals: 5

(i)
$$x(t) = e^{-a|t|}$$
 (ii) $x(t) = \frac{1}{a^2 + t^2}$ (iii) $x(t) = \cos \omega_0 t$ (10 Marks)

- State and prove the following properties in Fourier Transforms:
 - Differentiation property (Time)
 - (ii) Time shift property

(06 Marks)

Find the frequency response of the system and impulse response if differential equation of 6 the system is given by,

$$\frac{d^2}{dt^2}y(t) + 5\frac{d}{dt}y(t) + 6y(t) = -\frac{d}{dt}x(t)$$
(08 Marks)

The RC filter is characterized by following impulse response find out corresponding frequency response:

$$h(t) = \frac{1}{RC} e^{-t/RC} u(t)$$

For the above LTI system plot the magnitude curve.

(08 Marks)

Module-4

- Find the Discrete Time Fourier Transform (DTFT), of a rectangular pulse sequence given by x[n] = u[n] - u[n - N](08 Marks)
 - b. A causal discrete LTI system is described by,

$$y[n] - \frac{3}{4}y[n-1] + \frac{1}{8}y[n-2] = x[n]$$

- Determine frequency response of the system $H(\Omega)$.
- Find the impulse response h[n] of the system.

(08 Marks)

Use appropriate properties to find DTFT of the following signal: 8

(i)
$$x[n] = \left[\frac{1}{2}\right]^n u[n-2].$$

(ii)
$$x[n] = n\left[\frac{1}{2}\right]^{n}$$
 (08 Marks)

b. A discrete LTI first order system is given by,

$$y[n] = x[n] + x[n-1]$$

Find out the frequency response of the system and impulse response.

(08 Marks)

Module-5

9 a. Determine the z-transform, ROC and the location of poles and zeros of X(z) for the given x(n),

$$x(n) = -\left(\frac{1}{2}\right)^{n} u(-n-1) - \left(-\frac{1}{3}\right)^{n} u(-n-1).$$
 (08 Marks)

b. Use the method of partial fractions to obtain time domain signal corresponding to the given X(z).

$$X(z) = \frac{z^2 - 3z}{z^2 + \frac{3}{2}z - 1} \text{ ROC } \frac{1}{2}|z| < 2$$
 (08 Marks)

OR

- 10 a. What are the properties of Region Of Convergence (ROC) in z-transform? (04 Marks)
 - b. Find the inverse z transform of $X(z) = \ln(1+z^{-1})$ using power series expansion. (04 Marks)
 - c. Solve the following difference equation using unilateral z-transform:

$$y(n) - \frac{3}{2}y(n-1) + \frac{1}{2}y(n-2) = x(n)$$
 for $n \ge 0$

$$y(-1) = 4$$
, $y(-2) = 10$ and $x(n) = \left(\frac{1}{4}\right)^n u(n)$ (08 Marks)