

CBCS SCHEME

15EE63

Sixth Semester B.E. Degree Examination, June/July 2019 Digital Signal Processing

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Determine DFT of sequence $x(n) = \frac{1}{3}$ for $0 \leq n \leq 2$ for $N = 4$. Plot magnitude and phase spectrum. (08 Marks)
- b. Two length – 4 sequence are defined below :
- $$x(n) = \cos\left(\frac{\pi n}{2}\right) \quad n = 0, 1, 2, 3$$
- $$h(n) = 2^n \quad n = 0, 1, 2, 3$$
- i) Calculate $x(n) \otimes_4 h(n)$ using circular convolution directly.
- ii) Calculate $x(n) \otimes_4 h(n)$ using Linear convolution. (08 Marks)

OR

- 2 a. Compute circular convolution using DFT + IDFT for following sequence :
- $$x_1(n) = \left\{ \underset{\uparrow}{2}, 3, 1, 1 \right\}, \quad x_2(n) = \left\{ \underset{\uparrow}{1}, 3, 5, 3 \right\}.$$
- (08 Marks)
- b. Find the output of the LTI system whose impulse $h(n) = \{1, 1, 1\}$ and the input signal is $x(n) = \{3, -1, 0, 1, 3, 2, 0, 1, 2, 1\}$. Using the overlap save method. Use 6-pt circular convolution. (08 Marks)

Module-2

- 3 a. What are FFT algorithms? Explain the advantages of FFT algorithms over the direct computations of DFT for a sequence $x(n)$. (04 Marks)
- b. What are the differences and similarities between DIT and DIF –FFT algorithms? (04 Marks)
- c. Find the 8-pt DFT of the sequence $x(n) = \{1, 2, 3, 4, 4, 3, 2, 1\}$. Using DIT – FFT radix – 2 algorithm. (08 Marks)

OR

- 4 a. Find the 4-pt circular convolution of $x(n)$ and $h(n)$ given. Using radix-2 DIF – FFT algorithm. (08 Marks)

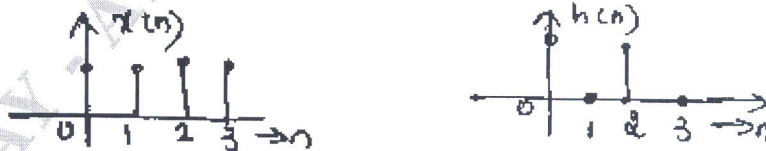


Fig.Q4(a)

- b. Given $x(n) = (n + 1)$ and $N = 8$. Determine $X(K)$. Using DIF – FFT algorithm. (08 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

Module-3

- 5 a. Convert the analog filter with system transfer function :

$$H(s) = \frac{(s + 0.1)}{(s + 0.1)^2 + 3^2}$$

into a digital IIR filter by mean of the impulse invariant method. (06 Marks)

- b. Design a butter worth digital IIR lowpass filter using bilinear transformation by taking $T = 0.1$ sec, to satisfy the following specification :

$$\begin{aligned} 0.6 \leq |H(e^{j\omega})| \leq 1.0; & \quad \text{for } 0 \leq \omega \leq 0.35\pi \\ |H(e^{j\omega})| \leq 0.1; & \quad \text{for } 0.7\pi \leq \omega \leq \pi \end{aligned} \quad (10 \text{ Marks})$$

OR

- 6 a. Compare analog and digital filters. (04 marks)
 b. Determine the poles of lowpass Butterworth filter for $N = 2$. Sketch the location of poles on s-plane and hence determine the normalized transfer function of lowpass filter. (08 Marks)
 c. Write difference between IIR and FIR filter. (04 Marks)

Module-4

- 7 a. Design a Chebyshev digital IIR lowpass filter using impulse invariant transformation by taking $T = 1$ sec to satisfy the following specifications;

$$\begin{aligned} 0.9 \leq |H(e^{j\omega})| \leq 1.0; & \quad \text{for } 0 \leq \omega \leq 0.25\pi \\ |H(e^{j\omega})| \leq 0.24; & \quad \text{for } 0.5\pi \leq \omega \leq \pi \end{aligned}$$

Draw direct form – I and II structure of the filter. (12 Marks)

- b. Write the relation between analog and digital frequency in Billnear transformation. (04 Marks)

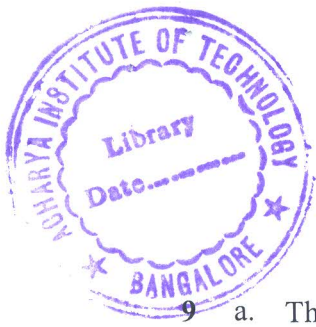
OR

- 8 a. Obtain the direct form – I, direct form II realization of the LTI system governed by the relation.

$$y(n) = -\frac{3}{8}y(n-1) + \frac{3}{32}y(n-2) + \frac{1}{64}y(n-3) + x(n) + 3x(n-1) + 2x(n-2). \quad (08 \text{ Marks})$$

- b. Realize the given system in cascade and parallel form :

$$H(z) = \frac{1 + 0.25z^{-1}}{(1 - 2z^{-1} + 0.25z^{-2})(1 - 3z^{-1} + 0.25z^{-2})}. \quad (08 \text{ Marks})$$

**Module-5**

- 9 a. The frequency response of a filter is described by : $H(\omega) = j\omega$, $-\pi \leq \omega \leq \pi$. Design the filter using a rectangular window. Take $N = 7$. (08 Marks)
- b. Design a lowpass digital filter to be used in A/D – H(z) – D/A structure that will have – 3dB cutoff at 30π rad/sec and attenuation factor of 5dB at 45π rad/sec. The filter is required to have a linear phase and the system will use sampling frequency of 100 samples/sec. (08 Marks)

OR

- 10 a. Deduce the equation for the following frequency spectrum for rectangular window sequence defined by :

$$w_f(n) = \begin{cases} 1, & \frac{-(N-1)}{2} \leq n \leq \frac{N-1}{2} \\ 0, & \text{otherwise} \end{cases} \quad (06 \text{ Marks})$$

- b. A lowpass filter has the desired frequency response :

$$H_d(\omega) = \begin{cases} e^{-j\omega^3}, & 0 < \omega < \pi/2 \\ 0, & \text{otherwise} \end{cases}$$

Determine $h(n)$ based on frequency sampling method. Take $K = 7$. (06 Marks)

- c. Realize the linear phase FIR filter having the following impulse response :

$$h(n) = \delta(n) + \frac{1}{4}\delta(n-1) - \frac{1}{8}\delta(n-2) + \frac{1}{4}\delta(n-3) + \delta(n-4). \quad (04 \text{ Marks})$$
