Second Semester M.Tech. Degree Examination, June/July 2018 Error Control Coding

Time: 3 hrs.

Max. Marks: 80

Note: Answer FIVE full questions, choosing ONE full question from each module.

Module-1

a. Define mutual information of the channel and state the properties.

(08 Marks)

b. Define a group, and construct the group under module-5 addition and multiplication over GF(5). (08 Marks)

OR

- 2 a. Define channel capacity of a discrete memory less channel consider a binary symmetric channel with equal source input probabilities, for conditional error probability of 'p' show that the channel capacity C is given by C = 1 H(p). (06 Marks)
 - b. Construct a table for $GF(2^4)$ based on the primitive polynomial $p(X) = 1 + X + X^4$. Display the power polynomial and vector representations of each element. (66 Marks)
 - c. Given the matrix G write the parity check matrix H and $G = \begin{bmatrix} 1 & 1 & 0 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$

Show that the raw space of G is the null space of H.

(04 Marks)

Module-2

- 3 a. For a systematic (7, 4) linear block code the priority matrix is given by P:
 - i) Draw the encoding circuit
 - ii) Draw the syndrome calculation circuit
 - iii) Detect and correct the error in the received vector $R = [1 \ 0 \ 1 \ 1 \ 1 \ 0 \ 0]$.

$$p = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 1 \end{bmatrix}.$$

(10 Marks)

b. Discuss the reed Muller code and its properties.

(06 Marks)

OR

4 a. For a (6, 3) linear code generated by the G matrix:

$$G = \begin{bmatrix} 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 0 & 0 & 1 \end{bmatrix}$$

- i) Construct the standard array (with one bit error)
- ii) Determine the probability of decoding error if the transition probability for a BSC is $p = 10^{-2}$
- iii) Correct any errors in the received vector. $\gamma_1 = (010110)$ and $\gamma_2 = (011101)$. (10 Marks)
- b. Construct the generator matrix and parity check matrix with n = 5 for
 - Single parity check code ii) Repetition code.

(06 Marks)

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Module-3

5 a. Design an encoder for a (7, 4) cyclic code with $g(x) = 1 + x + x^3$. Find the code word for the message (1010) with shift register contents. (06 Marks)

b. Write the decoding circuit for the (7, 4) cyclic code generated by $g(x) = 1 + x + x^3$. Describe the error correction process for the received word $\gamma = (1011011)$, shift into the shift register from left end. (10 Marks)

OR

6 a. Prove that an (n, k) linear code C is cyclic if every cyclic shift of a code word in C is also a code word in C. (06 Marks)

b. With a neat diagram explain the principle of operation of (31, 26) decoding circuit for a cyclic hamming code, generated by $g(x) = 1 + x^2 + x^5$ what modification is required for (28, 23) shortened cyclic code. (10 Marks)

Module-4

7 a. Describe the parameters of binary primitive BCH codes and determine g(x) for double error correction and triple error correction. (08 Marks)

b. Write the Galoisfield implementation of multiplying an arbitrary element in $GF(2^4)$ by 2^3 with $\phi(X) = 1 + X + X^4$. (68 Marks)

OR

- 8 a. Evaluate the syndrome for the double error correcting (15, 7) BIH code with received vector $\gamma = (1000\ 0000\ 1000\ 000)$.
 - b. With a neat block diagram explain the operational steps of general type II one step majority logic decoders.

 (08 Marks)

Module-5

- 9 a. i) Develop the convolutional encoder with k=4, rate $\frac{1}{2}$ $g_1(x) = 1 + x^2 + x^3$, $g_2(x) = 1 + x + x^2 + x^3$
 - ii) Determine the code word for the message m = 1101 with initial condition as zero.
 - b. Discuss the feedback decoding method to decode the convolutional code at the receiver.

 (06 Marks)

OR

- 10 a. Write the convolutional encoder with k=3, rate $\frac{1}{2}$ $g_1(x) = 1 + x + x^2$, $g_2(x) = 1 + x^2$
 - b. Write the state diagram
 - c. Write the decoding trellis diagram
 - d. Correct the error in the received sequence Z = 1101011001 using viter i algorithm.

(16 Marks)