



PART - 4

- 7 a. Obtain the reduction formula for  $\int \sin^n x \, dx$ . (07 Marks)
- b. Solve  $\sec x \tan x \tan y \, dx + \sec x \sec^2 y \, dy - e^x \, dx = 0$ . (06 Marks)
- c. Find the orthogonal trajectories of the family of curves  $r^n = a^n \cos n\theta$ . (07 Marks)
- 8 a. Evaluate :  $\int_0^{2a} x^3 \sqrt{2ax - x^2} \, dx$ . (07 Marks)
- b. Solve  $\frac{dy}{dx} + y \tan x = y^2 \sec x$ . (06 Marks)
- c. Suppose that an object is heated to  $300^\circ\text{F}$  and allowed to cool in a room whose air temperature is  $80^\circ\text{F}$ . After 10 minutes the temperature of the object is  $250^\circ\text{F}$ . What will be its temperature after 20 minutes? (07 Marks)

PART - 5

- 9 a. Find the rank of matrix :
- $$A = \begin{bmatrix} 2 & -1 & 3 & 4 \\ 0 & 3 & 4 & 1 \\ 2 & 3 & 7 & 5 \\ 2 & 5 & 11 & 6 \end{bmatrix}$$
- (06 Marks)
- b. Diagonalize the matrix  $A = \begin{bmatrix} 4 & 1 \\ 2 & 3 \end{bmatrix}$ . (07 Marks)
- c. Use power method to find the largest eigen value and the corresponding eigen vectors of  $A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$  taking initial eigen vectors  $[1, 1, 1]$ . (07 Marks)
- 10 a. Solve by Gauss elimination method :
- $$\begin{aligned} 4x + y + z &= 4 \\ x + 4y - 2z &= 4 \\ 3x + 2y - 4z &= 6. \end{aligned}$$
- (07 Marks)
- b. Show that transformation  $y_1 = 2x_1 + x_2 + x_3$   
 $y_2 = x_1 + x_2 + 2x_3$   
 $y_3 = x_1 - 2x_3$  is regular and find the inverse transformation. (06 Marks)
- c. Solve by LU decomposition method the equations :
- $$\begin{aligned} 3x + 2y + 7z &= 4 \\ 2x + 3y + z &= 5 \\ 3x + 4y + z &= 7. \end{aligned}$$
- (07 Marks)

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