

USN

--	--	--	--	--	--	--	--	--	--

13MCA41

**Fourth Semester MCA Degree Examination, June/July 2018**  
**Analysis & Design of Algorithms**

Time: 3 hrs.

Max. Marks:100

**Note: Answer any FIVE full questions.**

- 1**
- Explain worst case, best case and average case efficiencies. (06 Marks)
  - Solve the following recurrence relation,  
 $A(n) = A\left(\frac{n}{2}\right) + 1$  for  $n > 1$  by taking initial condition as  $A(1) = 0$  and  $n = 2^k$  (04 Marks)
  - Write algorithms for bubble sort and selection sort and give time complexities for both. (10 Marks)
- 2**
- Discuss algorithm design and analysis process. (04 Marks)
  - Explain asymptotic notations. (06 Marks)
  - Analysis time complexity of matrix multiplication. (06 Marks)
  - Define the following terms: (04 Marks)
    - Weighted graph
    - Connected graph.
    - Ordered tree
    - Dictionary
- 3**
- Illustrate how divide and conquer is applied using quicksort to the following numbers for sorting:  
65 70 75 80 85 60 55 50 45 (08 Marks)
  - Explain time complexity of Mergesort. (06 Marks)
  - Analysis time complexity of stressen's matrix multiplication. (06 Marks)
- 4**
- Explain general strategies applied in decrease and conquer technique. (04 Marks)
  - Write algorithm for Depth-First search. (06 Marks)
  - Illustrate source-removal algorithm for topological sorting problem. (06 Marks)
  - Write differences between DFS and BFS. (04 Marks)
- 5**
- Explain about input enhancement. (04 Marks)
  - Write Harspool's string matching algorithm. Apply this to find the pattern "BARBER" in the text "JIM-SAW ME-IN-A BARBER SHOP". (12 Marks)
  - Discuss about various types of hashing. (04 Marks)
- 6**
- Apply dynamic programming technique for the below knapsack problem and find the optimal value of the knapsack.  
 $n = 4$  (no. of items)  $W(\text{capacity}) = 5$  (10 Marks)
 

Item	1	2	3	4
Weight	2	1	3	2
Profit	12	10	20	15
  - Write Floyd's algorithm. (05 Marks)
  - Write an algorithm for computing the binomial coefficient  $C(n, K)$  using dynamic programming. (05 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
 2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

- 7 a. Write Prim algorithm and apply the same to find minimum cost spanning tree for the following graph. (10 Marks)

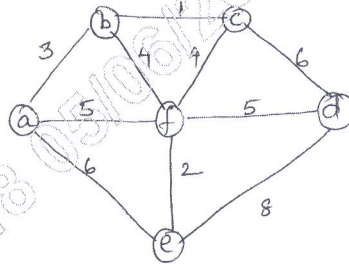


Fig. Q7 (a)

- b. Apply Dijkstra algorithm to the following graph: (05 Marks)

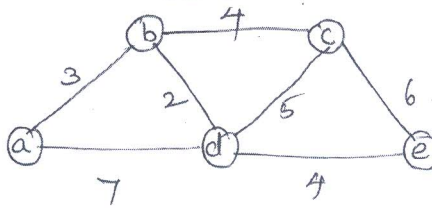


Fig. Q7 (b)

- c. Apply Branch-bound technique for knapsack problem by taking following values:  
 $n = 4$ ,  $m = 10$  (weight of knapsack)

$$(P_1, P_2, P_3, P_4) = (40, 42, 25, 12)$$

$$(W_1, W_2, W_3, W_4) = (4, 7, 5, 3)$$

(05 Marks)

- 8 a. Draw Decision trees for 3 elements selection sort and binary search in a four element array. (06 Marks)  
 b. Write algorithm for Back tracking and draw state-space tree for four queen's problem using back tracking. (08 Marks)  
 c. Explain about P, NP and NP-complete. (06 Marks)

\*\*\*\*\*