Third Semester B.E. Degree Examination, Dec.2018/Jan.2019

Mechanics of Materials

Time: 3 hrs.

Max. Marks: 100

Note: 1. Answer any FIVE full questions, selecting at least TWO questions from each part. 2. Missing data if any may be suitably assumed.

PART - A

Define: i) Poisson's ratio

ii) Lateral strain iv) Elasticity

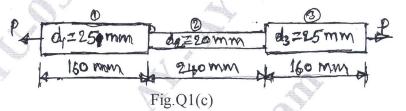
(04 Marks)

iii) Stress

b. Explain stress-strain diagram of mild-steel with salient features.

(06 Marks)

The bar shown in Fig.Q1(c) is tested in universal testing machine. It is observed that at a load of 40 kN the total extension of the bar is 0.285 mm. Determine the Young's modulus of the material.



(10 Marks)

2 Explain volumetric strain and obtain the expression for volumetric strain for a circular bar.

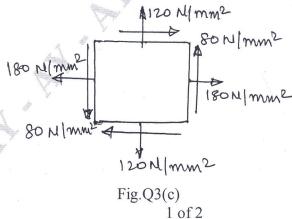
- b. Establish a relationship between the modulus of elasticity and modulus of rigidity. (06 Marks)
- A compound bar is made of a central steel plate 60 mm wide and 10 mm thick to which copper plates 40 mm wide by 5 mm thick are connected rigidly on each side. The length of the bar at normal temperature is 1 meter. If the temperature is raised by 80°C, determine the stresses in each metal and the change in length. Take $E_s = 200 \text{ GN/m}^2$, $E_c = 100 \text{ GN/m}^2$, $\alpha_s = 12 \times 10^{-6} / {}^{\circ}\text{C}, \ \alpha_c = 17 \times 10^{-6} / {}^{\circ}\text{C}.$ (10 Marks)
- Explain: (i) Plane stress
- (ii) Principal strain.

(04 Marks)

b. Derive an expression for an element subjected to uniaxial stress.

(06 Marks)

- c. The state of stress at a point in a strained material is shown in Fig.Q3(c). Determine:
 - i) The direction of the principal planes
 - ii) Magnitude of the principal stresses
 - iii) The magnitude of the maximum shear stress and its direction.



(10 Marks)

4 a. The bar with circular cross section as shown in Fig.Q4(a) is subjected to a load of 10 kN. Determine the strain energy stored in it. Take $E = 2.1 \times 10^5 \text{ N/mm}^2$.

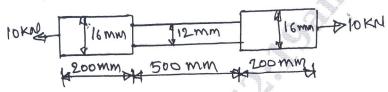


Fig.Q4(a)

(10 Marks)

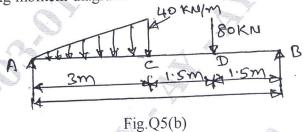
b. A pipe of 400 mm internal diameter and 100 mm thickness contains a fluid at a pressure 80 N/mm². Find the maximum and minimum hoop stresses across the section. Also sketch the radial and hoop stress distribution across the section. (10 Marks)

PART - B

5 a. Derive expressions relating load, shear force and bending moment with used notations.

(05 Marks)

b. A simply supported beam AB of 6 m span is loaded as shown in Fig.Q5(b). Draw the shear force and bending moment diagram.

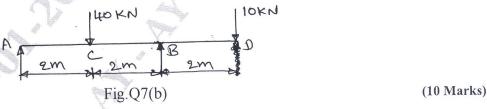


(15 Marks)

- 6 a. What are the assumptions made in simple theory of bending? (04 Marks)
 - b. Derive an expression for relationship between bending stress and radius of curvature.

(06 Marks)

- c. A cast iron beam has an I-section with top flange 80 mm × 40 mm, web 120 mm × 20 mm and bottom flange 160 mm × 40 mm. If tensile stress is not to exceed 30 N/mm² and compressive stress 90 N/mm², what is the maximum uniformly distributed load the beam can carry over a simply supported span of 6m if the larger flange is in tension. (10 Marks)
- 7 a. Derive an expression $EI \frac{d^2y}{dx^2} = M$ with usual notation. (10 Marks)
 - b. Determine the deflection under the loads in the beam shown in Fig.Q7(b). Take flexural rigidity as EI throughout.



- 8 a. Derive an expression $\frac{T}{I_p} = \frac{q}{r} = \frac{G\theta}{\ell}$ with usual notations. (10 Marks)
 - b. A hollow cast iron whose outside diameter is 200 mm and has a thickness of 20 mm is 4.5 m long and is fixed at both ends. Calculate the safe load by Rankine's formulae using factor of safety of 2.5. Find the ratio of Euler's to Rankine's load. Take $E = 1 \times 10^5 \text{ N/mm}^2$ and Rankine's constant = 1/1600 for both ends pinned case and $\sigma_c = 550 \text{ N/mm}^2$. (10 Marks)